



UNIVERSITY  
OF WARSAW



FACULTY OF  
ECONOMIC SCIENCES

## WORKING PAPERS

No. 23/2023 (430)

# MEAN ABSOLUTE DIRECTIONAL LOSS AS A NEW LOSS FUNCTION FOR MACHINE LEARNING PROBLEMS IN ALGORITHMIC INVESTMENT STRATEGIES

JAKUB MICHAŃKÓW  
PAWEŁ SAKOWSKI  
ROBERT ŚLEPACZUK

WARSAW 2023



## Mean Absolute Directional Loss as a New Loss Function for Machine Learning Problems in Algorithmic Investment Strategies

*Jakub Michańków<sup>a,b</sup>, Paweł Sakowski<sup>b</sup>, Robert Ślepaczuk<sup>b</sup>*

<sup>a</sup> *Cracow University of Economics, Department of Informatics*

<sup>b</sup> *University of Warsaw, Faculty of Economic Sciences, Quantitative Finance Research Group, Department of Quantitative Finance*

*Corresponding author: rslepaczuk@wne.uw.edu.pl*

---

**Abstract:** This paper investigates the issue of an adequate loss function in the optimization of machine learning models used in the forecasting of financial time series for the purpose of algorithmic investment strategies (AIS) construction. We propose the Mean Absolute Directional Loss (MADL) function, solving important problems of classical forecast error functions in extracting information from forecasts to create efficient buy/sell signals in algorithmic investment strategies. Finally, based on the data from two different asset classes (cryptocurrencies: Bitcoin and commodities: Crude Oil), we show that the new loss function enables us to select better hyperparameters for the LSTM model and obtain more efficient investment strategies, regarding risk-adjusted return metrics on the out-of-sample data.

---

**Keywords:** machine learning, recurrent neural networks, long short-term memory, algorithmic investment strategies, testing architecture, loss function, walk-forward optimization, over-optimization

**JEL codes:** C4, C14, C45, C53, C58, G13

**Acknowledgements:** This document is the results of the research project funded by IDUB program: BOB-IDUB-622-233/2022 at the University of Warsaw.

### ORCID ID:

- Jakub Michańków: 0000-0002-0567-6240
- Paweł Sakowski: 0000-0003-3384-3795
- Robert Ślepaczuk: 0000-0003-3384-3795

## 1. Introduction

The main idea for this paper comes from the unsolved dilemma regarding the search for forecasting models that can be used for buy/sell signal generation in algorithmic investment strategies (AIS). No matter what kind of theoretical concept is incorporated into the heart of such an investment model, we have a few similar issues that have to be properly addressed to increase the probability of generating efficient signals on out-of-sample (OOS) data. Among many others, these include the architecture of testing various models (machine learning, econometric, macroeconomic, or statistical approaches), the structure of the walk-forward procedure (usually consisting of numerous training, validation, and testing periods of different lengths), hyperparameters tuning and parameters optimization, model estimation phase, and finally the appropriate set of time series with possibly diverse characteristics of their distributions. The point is that all of these problems have to be designed optimally in order to avoid potential over-fitting issues and find the best possible variant of the investment model.

Majority of papers undertaking the topic of AIS testing do not put proper attention to these problems and focus only on the empirical testing of one or several selected investment models, on a single instrument, over quite short data periods, usually without explaining the details of the whole procedure. In this paper, we decided to focus on one crucial aspect of testing such models, which is, in our opinion, the selection of a proper loss function. In reality, it has the greatest impact on hyper-parameter tuning, followed by the model estimation phase.

The main hypothesis verified in this paper is as follows (RH): *The MADL loss function has better properties than classical forecast error functions in the optimization of ML models used in forecasting financial time series for the purpose of AIS construction.* In order to verify this hypothesis, after a brief reference to the most common drawbacks in papers testing AIS (Literature Review section), and a description of our architecture of testing (Methodology and Data section), we define and describe the new formula of the MADL function, focusing primarily on its conceptual differences to other similar functions. Then, in the Results section, we show the empirical comparison of the use of the MADL function and the classical forecast error function (MAE) on two various time series: Bitcoin and Crude Oil daily simple returns. In this analysis, we visualize potential differences in a more realistic way than only theoretical deliberations. Finally, we conclude and present some extensions of this research.

## 2. Literature review

The literature review presented below focuses on critical drawbacks in papers that describe the testing of algorithmic investment strategies. The main issue is that the vast majority of these papers do not maintain a proper testing structure, which is why their results cannot be treated as valid and robust, despite the fact that the literature on this topic is very broad. Prior to moving on to the main part of this study, it is crucial to list and describe the most frequent flaws in papers examining different AIS. These include:

- Over-optimization of machine learning models (Lopez de Prado (2013), Bailey et al. (2016b)).
- Wrong optimization criteria or loss functions, including RMSE, MSE, MAE, MAPE, percent of over-predictions (%OP), and others. These are used by authors in a vast majority of publications, making it hard to choose the optimal methods for producing buy/sell signals (Di Persio and Honchar (2016), Yang et al. (2019)).
- Only one in-sample period and one out-of-sample period, making the results highly dependent on the chosen period. A great number of research papers on this topic (Wiecki et al. (2016), Lopez de Prado (2013), Bailey et al. (2016b), Raudys (2016)) highlight this issue as being very prevalent.
- Because there was no out-of-sample period, the paper's findings lack any forecasting ability (Topcu and Gulal (2020), Caporale and Plastun (2019)).
- As there is only one basis instrument used for AIS testing, the distributional characteristics of this instrument have a strict influence on the results (Vo and Yost-Bremm (2020)).

- Forward-looking bias in buy/sell signals, which is typically caused by the use of future macroeconomic data or mistakes in the definitions of buy/sell signals (Chan (2013), Chan (2021), Jansen (2020))
- Lack of sensitivity analysis, which is essential in assessing robustness of model's results, with regard to the parameters that were initially chosen (Di Persio and Honchar (2016), Zhang et al. (2018), and Yang et al. (2019).
- Data snooping bias - when authors publish only their best results, without conducting a systematic examination of other parameters and assumptions (Bailey et al. (2016a), Chan (2013)).
- Survivorship bias - the selection of current index constituents, for instance, in research using data from the previous 20 years, is the most prevalent illustration of this bias (Chan (2021)).
- Inadequate performance metrics or their incorrect interpretation - the efficiency of investment strategies is evaluated only on the quality of point forecasts generated using the theoretical models that form the basis of such investment strategies, rather than of proper risk-adjusted return metrics calculated on the equity lines generated by these strategies (Chakole et al. (2021), Grobys et al. (2020)).

Some of the above mentioned drawbacks can be mitigated, at least in part, by pertinent testing of the model architecture. Special attention has to be paid to the hyperparameter tuning phase, where an appropriately selected loss function is critical.

### 3. Methodology and Data

#### 3.1. MADL. New Loss Function

We introduce our novel loss function to address one of the most prevalent issues with papers testing algorithmic trading strategies. In this study, we use it to enhance the predictive power of the LSTM model (Hochreiter and Schmidhuber (1997)) for these strategies.

Based on prior studies (e.g. Vo and Ślepaczuk (2022)), we came to the conclusion that popular error metrics like RMSE, MSE, MAE, MAPE, and %OP used in the majority of similar studies are not appropriate error functions for assessing the effectiveness of the models' forecasting abilities in AIS. The reason for this is that the error metrics mentioned above do not consider the forecasting ability of investment signals that are based on these forecasts; rather, they only consider the forecasting accuracy of forecasts (i.e., the difference between the forecasted and observed value). It implies that almost all of these error metrics (RMSE, MSE, MAE, and MAPE) penalize forecast errors regardless of whether they are positive or negative (forecast error =  $\hat{R}_i - R_i$ ), whereas the %OP metric only considers the forecast error's direction and not its magnitude. For this reason, researchers in the majority of other papers choose the signal combination that optimizes only the chosen error metric, rather than the most profitable combination of signals for the strategy.

To solve this problem, we suggest a new loss function, called Mean Absolute Directional Loss (MADL), which can be computed using the formula below:

$$\text{MADL} = \frac{1}{N} \sum_{i=1}^N (-1) \times \text{sign}(R_i \times \hat{R}_i) \times \text{abs}(R_i), \quad (1)$$

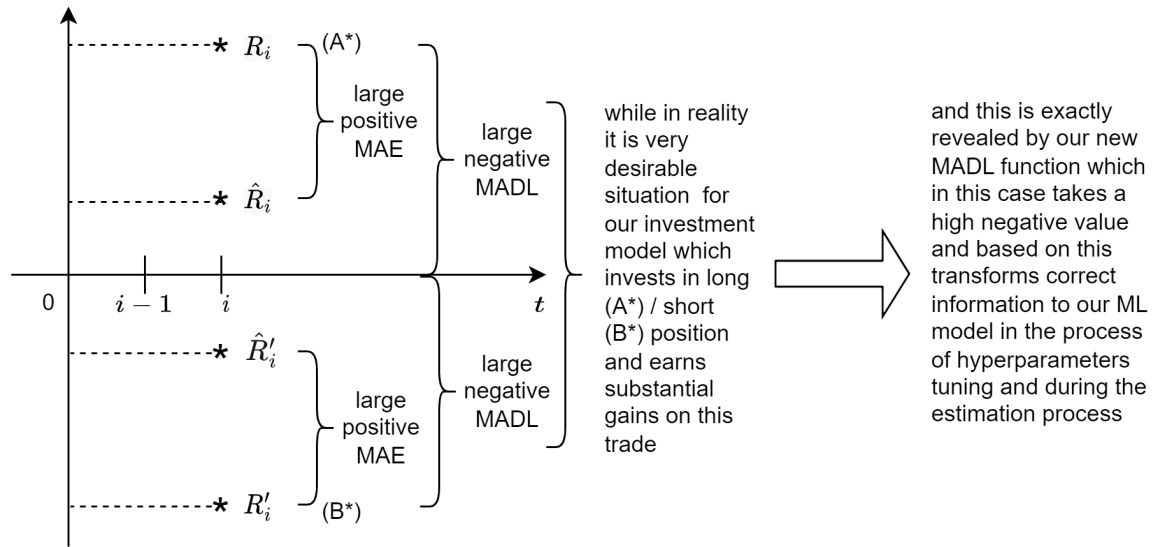
where MADL is the Mean Absolute Directional Loss,  $R_i$  is the observed return on interval  $i$ ,  $\hat{R}_i$  is the predicted return on the interval  $i$ ,  $\text{sign}(X)$  is the function that returns -1,0,1 as the sign of  $X$ ,  $\text{abs}(X)$  is the function that gives the absolute value of  $X$  and  $N$  is the number of forecasts. In this manner, the value the function returns will be equal to the observed return on investment with the predicted direction, allowing the model to determine whether the prediction will result in profit or loss and the amount of this profit or loss. MADL was designed specifically for generating signals for AIS. In our model, this function is minimized, ensuring that the strategy will produce a profit if it returns negative values and loss if it returns positive

values. MADL was also the main loss function used in hyperparameters tuning and in the estimation of the LSTM model.

In order to reveal the properties of the MADL function and visualize its differences with regard to classical error metrics (e.g. MAE) we present its main distinguishing characteristics, shown in three consecutive figures (Figure 1, 2, and 3).

Figure 1 depicts the difference between MAE and MADL logic that is responsible for the large differences between these two loss functions.

1\*) if  $\hat{R}_i * R_i > 0$  and  $R_i$  is significantly different than  $\hat{R}_i$  or than 0 => MAE is always large and penalizes such a model

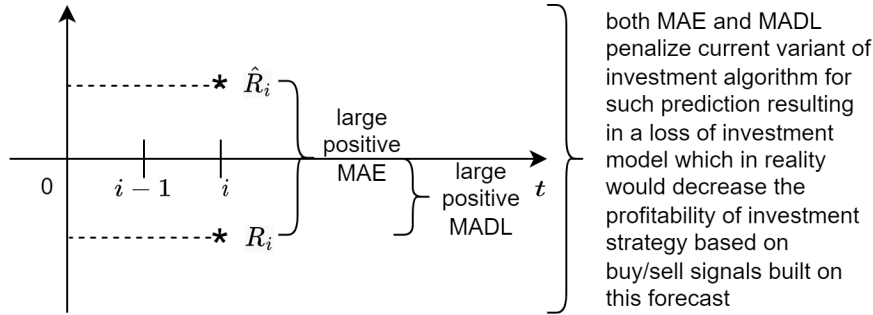


Note: Variants (A\*), and (B\*) show that in specific cases the difference between MAE and MADL values can be significant, and therefore affect the final selection of model parameters.

Figure 1: The difference between MAE and MADL logic #1.

Figure 2 presents the difference between MAE and MADL logic in the case when the difference is relatively small but still affects the final values of the loss functions.

2\*) if  $\hat{R}_i * R_i < 0$  and  $R_i$  is significantly different than  $\hat{R}_i$  or than 0 => MAE is always large and penalizes such a model, but this time similar indication is given by MADL and then these two loss functions evaluate the situation correctly

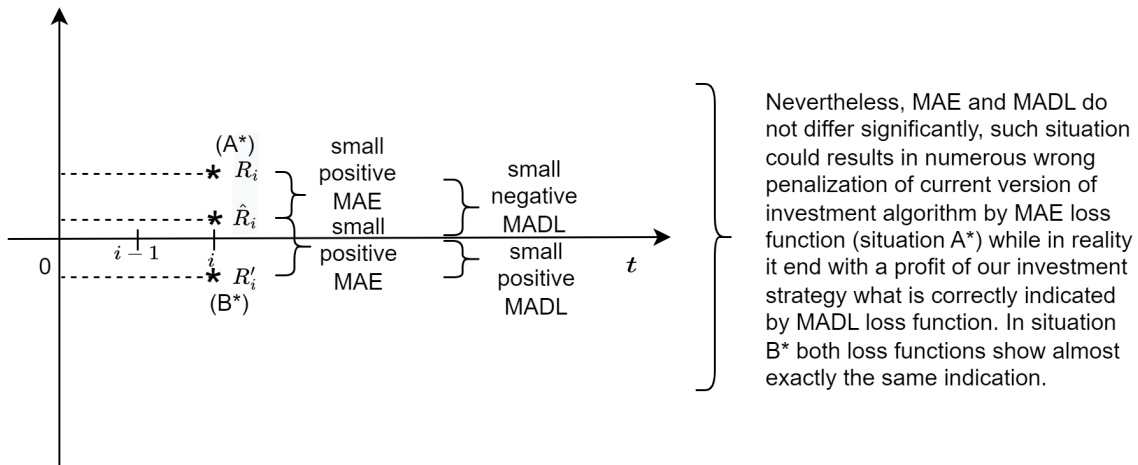


Note: This variant depicts the difference between MAE and MADL by treating the error as the distance between the predicted and observed values (MAE) and the observed and 0 (MADL) in cases where the sign of the prediction is not the same.

Figure 2: The difference between MAE and MADL logic #2.

Figure 3 presents the difference between MAE and MADL logic in the case when predicted and observed returns have an opposite sign and their values are significantly different.

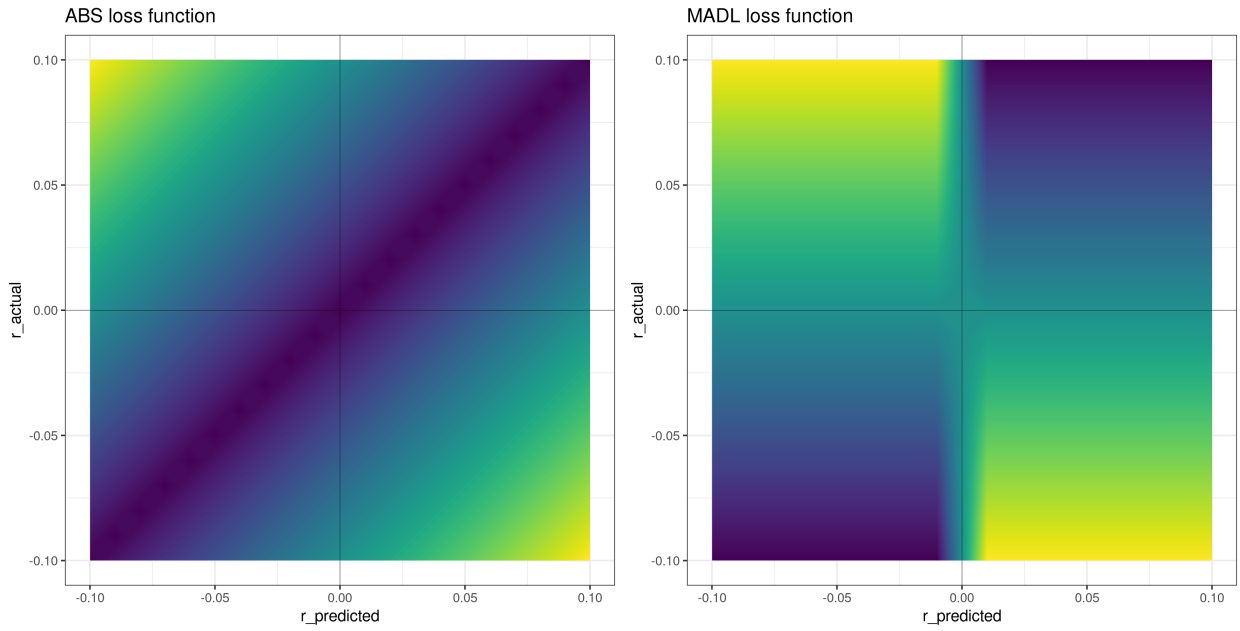
3\*) if  $\{(A^*) \hat{R}_i * R_i > 0 \text{ or } (B^*) \hat{R}_i * R_i < 0\}$  and  $R_i$  is not significantly different than  $\hat{R}_i$  or than 0 => MAE and MADL have similar absolute value but different sign ( $A^*$ ) or MAE and MADL do not differ significantly ( $B^*$ )



Note: The last example of the difference is negligible with regard to its value for a single prediction, but taking into account that we can have quite a few of them, it can substantially influence the aggregated value of the selected loss function.

Figure 3: The difference between MAE and MADL logic #3.

Figures (Figure 1, 2, and 3) show the most important conceptual differences between classical error functions and MADL. Additionally, Figure 4 presents the distribution of error in cases of large and small differences of observed return ( $R_i$ ) from predicted return ( $\hat{R}_i$ ) or from zero. What is significant about the MADL loss function is that the reference point for loss measurement is set to zero, whereas, in almost all other classical error metrics, it is the predicted return ( $\hat{R}_i$ ). Figure 4 presents the comparison of MAE and MADL for various values of predicted and observed returns.



Note: Dark blue color indicates the lowest error, while yellow color indicates the highest error. The left panel (with MAE) shows that the error is strictly dependent on the difference between  $\hat{R}_i$  and  $R_i$  while the right panel shows that  $\hat{R}_i$  is always compared with the zero reference point in the process of error calculation.

Figure 4: Loss functions: MADL vs MAE

### 3.2. Architecture of testing and research description

Before we move to the empirical part, it is important to describe the proper architecture for testing ML models used for AIS construction. Although the main aim of this paper is the presentation of the concept and main characteristics of the new loss function, the empirical part (see Section 4) with the testing example is added for visualization purposes and as an explanation of its use in practice. Figure 5 presents the process used in order to explain how exactly our AIS was tested.

We used the LSTM model with a walk-forward procedure of testing. The hyperparameters tuning phase was performed on the first in-sample period, then we trained and estimated our model on the remaining data. For this purpose, we used various combinations of the loss functions in order to extract information about the usefulness of the selected loss function in such a procedure. Table 1 summarizes the values of hyperparameters selected in the tuning phase for each loss function separately.

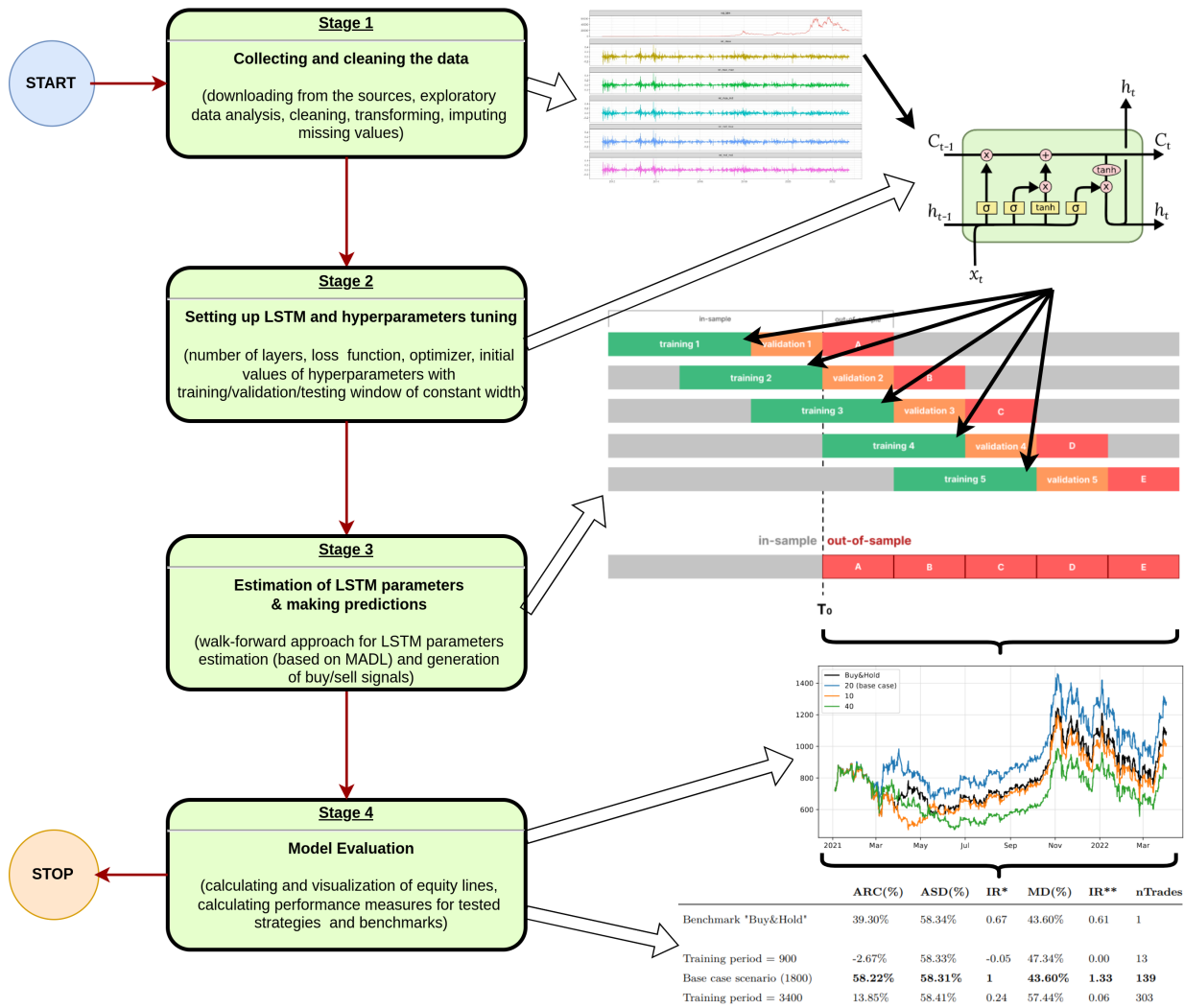


Figure 5: The process of LSTM model testing with MADL function



Table 1: Selected values of hyperparameters.

Hyperparameter	Selected Value MADL	Selected Value MAE
No. hidden layers	3	3
No. neurons	512/256/128	64/32/16
Activation function	tanh	tanh
Recurrent Activation	sigmoid	sigmoid
Dropout rate	0.02	0.0002
l2 regularizer	0.0005	0.00001
Optimizer	Adam	Adam
Learning rate	2.15	0.0015
BTC train/test	1460/365	1460/365
USO train/test	1008/252	1008/252
Batch size (BTC/USO)	1460/1008	1460/1008
Sequence length (BTC/USO)	20/10	20/10
Epochs	300	200

Note: MADL hyperparameters (second column) were used for MADL/MADL and MADL/MAE strategies, while MAE hyperparameters were used for MAE/MAE and MAE/MADL strategies.

Finally, we performed the following steps in order to perform the empirical part of this research:

- The division of data into in-sample (training and validation) and out-of-sample (test) sets, each with 1460/365 observations for BTC and 1008/252 observations for Crude Oil.
- Hyperparameters tuning based on new Loss function: MADL, described in Section 3.1, and the old concept of MAE, described above.
- Buy/Sell signals were generated based on the sign of next-day forecasts.
- Tests for one type of strategy: Long/Short.
- Walk-forward approach was used for testing.
- Equity lines and performance metrics from the two loss functions and assets according to Ślepaczuk et al. (2018), results provided in Section 4.

### 3.3. Performance Metrics

In order to evaluate the efficiency of tested strategies, we calculate the following performance metrics based on Kosc et al. (2019) and Bui and Ślepaczuk (2021). The performance metrics were divided into four categories:

- return performance metrics: Annualized Return Compounded (ARC)
- risk performance metrics: Annualized Standard Deviation (ASD), Maximum Drawdown (MD), Maximum Loss Duration (MLD)
- risk-adjusted return performance metrics: Information Ratio (IR\*), Modified Information Ratio (IR\*\*), Aggregated Information Ratio (IR\*\*\*)
- informative performance metrics: Number of observations (nObs), Number of trades (nTrades).

### 3.4. Data

We decided to use simple returns based on daily data of two assets from various asset classes: Bitcoin (BTC) and Crude Oil (represented by ETF named USO). The data we used covered the period from April 1, 2023 to December 31, 2021. Source of the BTC data: Kraken, Bitfinex, BTC-e, CEX, and Coinbase exchanges, while USO data was obtained from stooq.com.

#### 4. Results

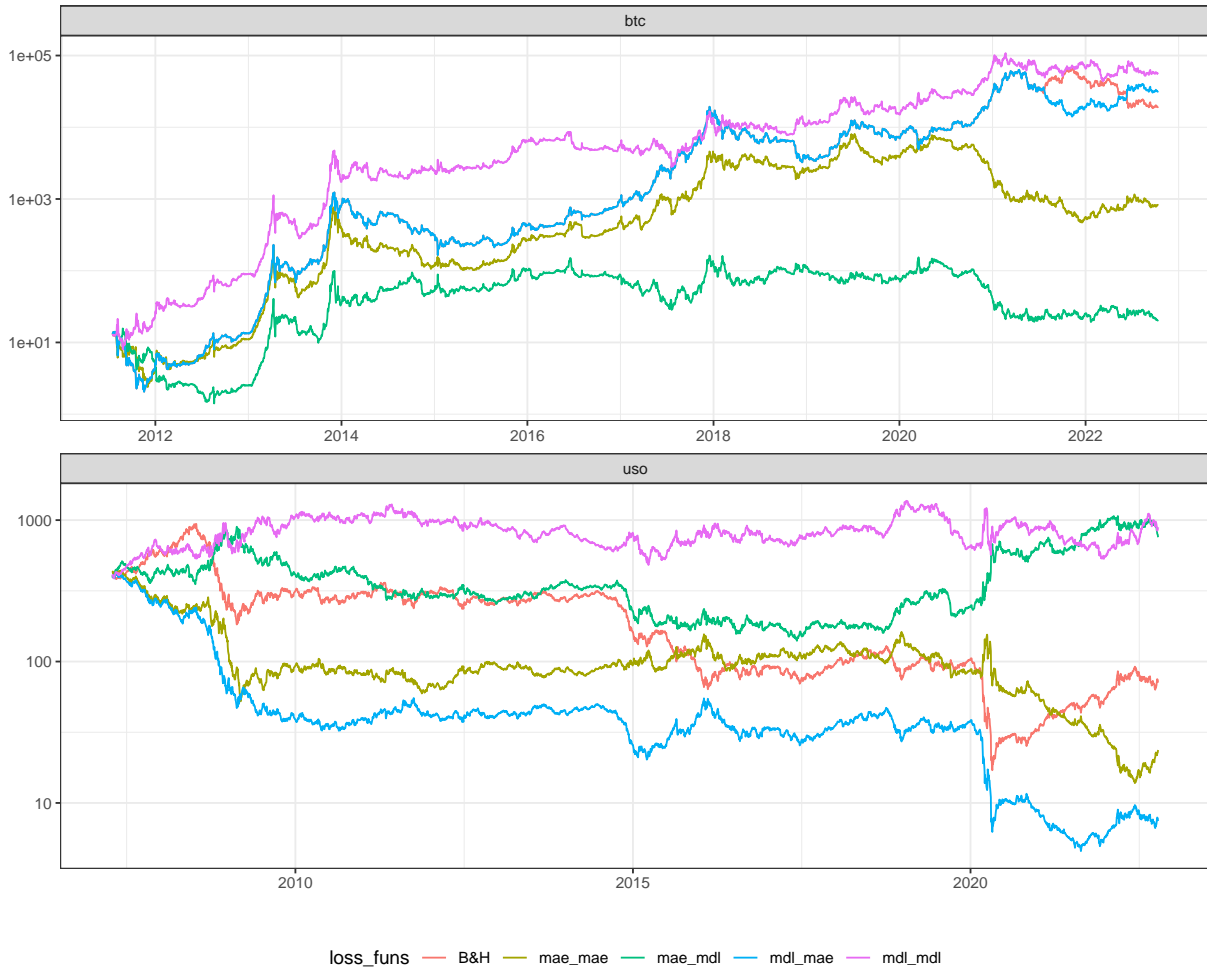
Table 2 presents the results of the LSTM model used in this research, for which the hyperparameters tuning, training, and estimation were performed based on various combinations of loss functions: MADL/MADL, MADL/MAE, MAE/MAE, and MAE/MADL. The performance metrics for final equity lines show that no matter which risk-adjusted return metrics ( $IR^*$ ,  $IR^{**}$ , and  $IR^{***}$ ) we select, the result is always the best in s of MADL/MADL approach.

Table 2: Comparison of two approaches

Model	aRC	aSD	MD	MLD	$IR^*$	$IR^{**}$	$IR^{***}$	nObs	nTrades
Panel A - BTC									
B&H	91.25	87.37	86.67	3.24	1.04	1.100	0.310	4107	2
MADL/MADL	109.94	87.34	75.04	1.91	1.26	1.844	1.062	4107	306
MADL/MAE	99.90	87.36	86.67	3.24	1.14	1.318	0.406	4107	4
MAE/MAE	44.26	87.45	94.18	3.46	0.51	0.238	0.030	4107	330
MAE/MADL	4.05	87.51	90.99	4.83	0.05	0.002	0.000	4107	320
Panel B - USO									
BH	-10.59	38.09	98.19	14.24	-0.28	-0.030	0.000	3901	2
MADL/MADL	5.25	38.08	62.73	7.58	0.14	0.012	0.000	3901	731
MADL/MAE	-22.70	38.07	98.91	15.42	-0.60	-0.137	-0.002	3901	11
MAE/MAE	-17.02	38.08	96.88	15.42	-0.45	-0.079	-0.001	3901	402
MAE/MADL	4.19	38.08	84.39	12.74	0.11	0.005	0.000	3901	692

Note: Panel A presents results for BTC, while panel B present the results for USO.

Figure 6 presents the fluctuations of equity lines of for BTC and USO in two panels (top: BTC and bottom: USO). Figure 6 which shows the best results for MADL/MADL can be treated as an additional confirmation of numeric results presented in Table 2.



Note: Equity lines present the fluctuations of investment strategies for BTC (upper panel) and USO (lower panel) for strategies trained based on various combinations of loss functions used (MAE/MAE, MAE/MADL, MADL/MAE, MADL/MADL) in the period between April 1, 2023, and December 31, 2021. Additionally, we included Buy & Hold (B&H) strategy as a benchmark strategy for comparison purposes.

Figure 6: Equity lines.

Table 3 presents the results of a test of significance of  $\alpha$  and  $\beta$  coefficients from the regression in the form of  $R_t = \alpha + \beta R_t^* + \varepsilon_t$ , where  $R_t$  is the buy and hold returns, and  $R_t^*$  returns from Long/Short strategy. The results presented in Table 3 confirm those presented in Table 2, with positive and significant  $\alpha$  for MADL/MADL strategy in case of BTC and confirm only partly MADL/MADL strategy for USO (positive  $\alpha$  but not significant).

## 5. Conclusions

This paper aimed to introduce the new concept of a more accurate loss function, which is appropriately adjusted to the problem of the optimization of machine learning models used in the forecasting of financial time series, and for construction of algorithmic investment strategies (AIS). For this purpose, we proposed a new loss function – MADL (Mean Absolute Directional Loss), presented the rationale for its construction, and a detailed interpretation with special attention to its difference with regard to classical loss functions used in the literature. Last but not least, we demonstrated how the new loss function helps us choose

Table 3: Results of regressions for returns: B&amp;H vs. MAE/MAE, MAE/MADL, MADL/MAE, MADL/MADL.

Dep. var.	Alpha	StdErr	$t$	pv	Beta	StdErr	$t$	pv
Panel A - BTC								
MAE/MAE	0.0009	0.001	1.431	0.152	0.394	0.014	27.4	0.000
MAE/MADL	0.0007	0.001	1.014	0.310	0.159	0.015	10.2	0.000
MADL/MAE	0.0004	0.000	1.307	0.191	0.895	0.007	129.0	0.000
MADL/MADL	0.0029	0.001	4.027	0.000	0.073	0.016	4.6	0.000
Panel B - USO								
MAE/MAE	-0.0005	0.000	-1.423	0.154	-0.374	0.015	-25.1	0.000
MAE/MADL	0.0004	0.000	1.104	0.269	-0.236	0.016	-15.1	0.000
MADL/MAE	-0.0006	0.000	-1.956	0.050	0.491	0.014	35.1	0.000
MADL/MADL	0.0004	0.000	1.215	0.224	-0.228	0.016	-14.6	0.000

Note: The table presents the results of regressions in the form of:  $R_t = \alpha + \beta R_t^* + \varepsilon_t$ , where  $R_t$  is the return for tested strategy in period  $t$  and  $R_t^*$  is the return in of BTC or USO strategies. Regressions were calculated in the period between April 1, 2023 to December 31, 2021. The hyperparameters of LSTM model for the base case scenario were set as it was described in Table 1.

better hyperparameters for our ML models and produce more effective investment strategies in terms of risk-adjusted return metrics on the out-of-sample data using two different asset classes (cryptocurrencies: Bitcoin and commodities: Crude Oil).

In the next step we intend to modify the original MADL loss function introducing various penalization structures, e.g. "squared" instead of "absolute" which could stress the problem of large losses in the process of optimization. Such modification could help us with training of various ML models responsible for forecasts used in the buy/sell signals generation process.

## References

- D. H. Bailey, J. Borwein, M. Lopez de Prado, A. Salehipour, and Q. J. Zhu. Backtest overfitting in financial markets. *Automated Trader*, 2016a.
- D. H. Bailey, J. Borwein, M. Lopez de Prado, and Q. J. Zhu. The probability of backtest overfitting. *Journal of Computational Finance*, forthcoming, 2016b.
- Q. Bui and R. Ślepaczuk. Applying hurst exponent in pair trading strategies on nasdaq 100 index. *Physica A: Statistical Mechanics and its Applications*, page 126784, 2021. ISSN 0378-4371. doi: <https://doi.org/10.1016/j.physa.2021.126784>. URL <https://www.sciencedirect.com/science/article/pii/S037843712100964X>.
- G. M. Caporale and A. Plastun. The day of the week effect in the cryptocurrency market. *Finance Research Letters*, 31, 2019. ISSN 1544-6123. doi: <https://doi.org/10.1016/j.frl.2018.11.012>. URL <https://www.sciencedirect.com/science/article/pii/S1544612318304240>.
- J. B. Chakole, M. S. Kolhe, G. D. Mahapurush, A. Yadav, and M. P. Kurhekar. A q-learning agent for automated trading in equity stock markets. *Expert Systems with Applications*, 163:113761, 2021. ISSN 0957-4174. doi: <https://doi.org/10.1016/j.eswa.2020.113761>. URL <https://www.sciencedirect.com/science/article/pii/S0957417420305856>.
- E. Chan. *Algorithmic trading: winning strategies and their rationale*, volume 625. John Wiley & Sons, 2013.
- E. P. Chan. *Quantitative trading: how to build your own algorithmic trading business*. John Wiley & Sons, 2021.
- L. Di Persio and O. Honchar. Artificial neural networks architectures for stock price prediction: Comparisons and applications. *International Journal of Circuits, Systems And Signal Processing*, 10:403–413, Jan. 2016.
- K. Grobys, S. Ahmed, and N. Sapkota. Technical trading rules in the cryptocurrency market. *Finance Research Letters*, 32:101396, 2020. ISSN 1544-6123. doi: <https://doi.org/10.1016/j.frl.2019.101396>. URL <https://www.sciencedirect.com/science/article/pii/S1544612319308852>.
- S. Hochreiter and J. Schmidhuber. Long Short-Term Memory. *Neural Computation*, 9(8):1735–1780, Nov. 1997. ISSN 0899-7667. doi: [10.1162/neco.1997.9.8.1735](https://doi.org/10.1162/neco.1997.9.8.1735). URL <https://doi.org/10.1162/neco.1997.9.8.1735>.
- S. Jansen. *Machine Learning for Algorithmic Trading: Predictive models to extract signals from market and alternative data for systematic trading strategies with Python*. Packt Publishing Ltd, 2020.
- K. Kosc, P. Sakowski, and R. Ślepaczuk. Momentum and contrarian effects on the cryptocurrency market. *Physica A: Statistical Mechanics and its Applications*, 523:691–701, June 2019. ISSN 0378-4371. doi: [10.1016/j.physa.2019.02.057](https://doi.org/10.1016/j.physa.2019.02.057). URL <https://www.sciencedirect.com/science/article/pii/S037843711930216X>.
- M. Lopez de Prado. What to look for in a backtest. *Available at SSRN*, 2013.

- A. Raudys. Portfolio of global futures algorithmic trading strategies for best out-of-sample performance. In *International Conference on Business Information Systems*, pages 424–435. Springer, 2016.
- M. Topcu and O. S. Gulal. The impact of covid-19 on emerging stock markets. *Finance Research Letters*, 36:101691, 2020. ISSN 1544-6123. doi: <https://doi.org/10.1016/j.frl.2020.101691>. URL <https://www.sciencedirect.com/science/article/pii/S1544612320306966>.
- A. Vo and C. Yost-Bremm. A high-frequency algorithmic trading strategy for cryptocurrency. *Journal of Computer Information Systems*, 60(6):555–568, 2020.
- N. Vo and R. Ślepaczuk. Applying hybrid arima-sgarch in algorithmic investment strategies on s&p500 index. *Entropy*, 24(2), 2022. ISSN 1099-4300. doi: 10.3390/e24020158. URL <https://www.mdpi.com/1099-4300/24/2/158>.
- T. Wiecki, A. Campbell, J. Lent, and J. Stauth. All that glitters is not gold: Comparing backtest and out-of-sample performance on a large cohort of trading algorithms. *The Journal of Investing*, 25(3):69–80, 2016.
- J. Yang, Y. Li, X. Chen, J. Cao, and K. Jiang. Deep Learning for Stock Selection Based on High Frequency Price-Volume Data. *arXiv:1911.02502 [cs, q-fin]*, Nov. 2019. URL <http://arxiv.org/abs/1911.02502>. arXiv: 1911.02502.
- R. Zhang, C. Huang, W. Zhang, and S. Chen. Multi Factor Stock Selection Model Based on LSTM. *International Journal of Economics and Finance*, 10(8):1–36, 2018. URL <https://ideas.repec.org/a/ibn/ijefaa/v10y2018i8p36.html>. Publisher: Canadian Center of Science and Education.
- R. Ślepaczuk, P. Sakowski, and G. Zakrzewski. Investment Strategies that Beat the Market. What Can We Squeeze from the Market? *Financial Internet Quarterly (formerly e-Finance)*, 14(4):36–55, 2018. URL <https://ideas.repec.org/a/vrs/finiqu/v14y2018i4p36-55n8.html>. Publisher: Sciendo.



UNIVERSITY OF WARSAW

FACULTY OF ECONOMIC SCIENCES

44/50 DŁUGA ST.

00-241 WARSAW

[WWW.WNE.UW.EDU.PL](http://WWW.WNE.UW.EDU.PL)