

Microeconomics

Lecture 5

Exchange Economies (revisited)

- ◆ **No production, only endowments, so no description of how resources are converted to consumables.**
- ◆ **General equilibrium: all markets clear simultaneously.**
- ◆ **1st and 2nd Fundamental Theorems of Welfare Economics.**

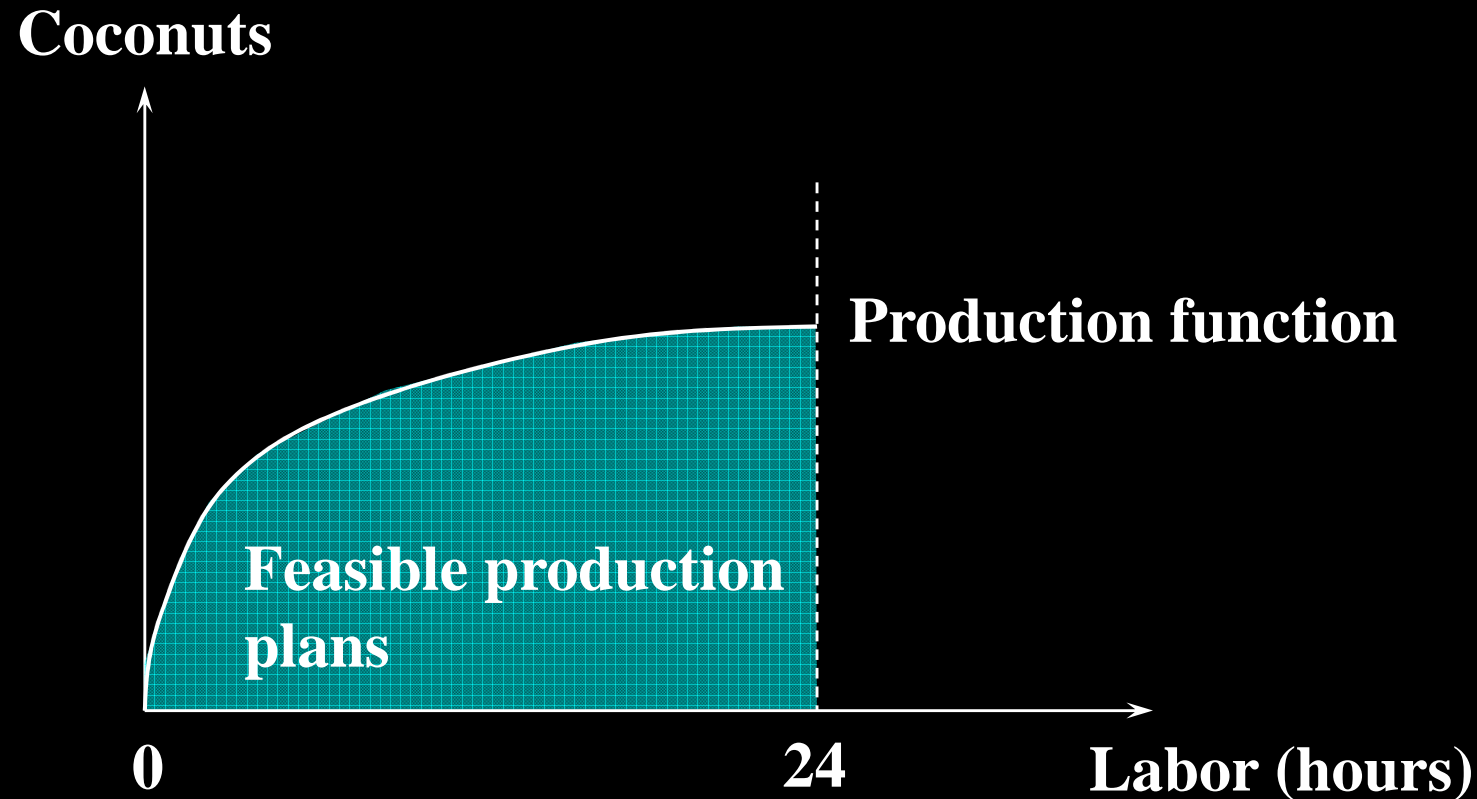
Now Add Production ...

- ◆ Add input markets, output markets, describe firms' technologies, the distributions of firms' outputs and profits ... **That's not easy!**

Robinson Crusoe's Economy

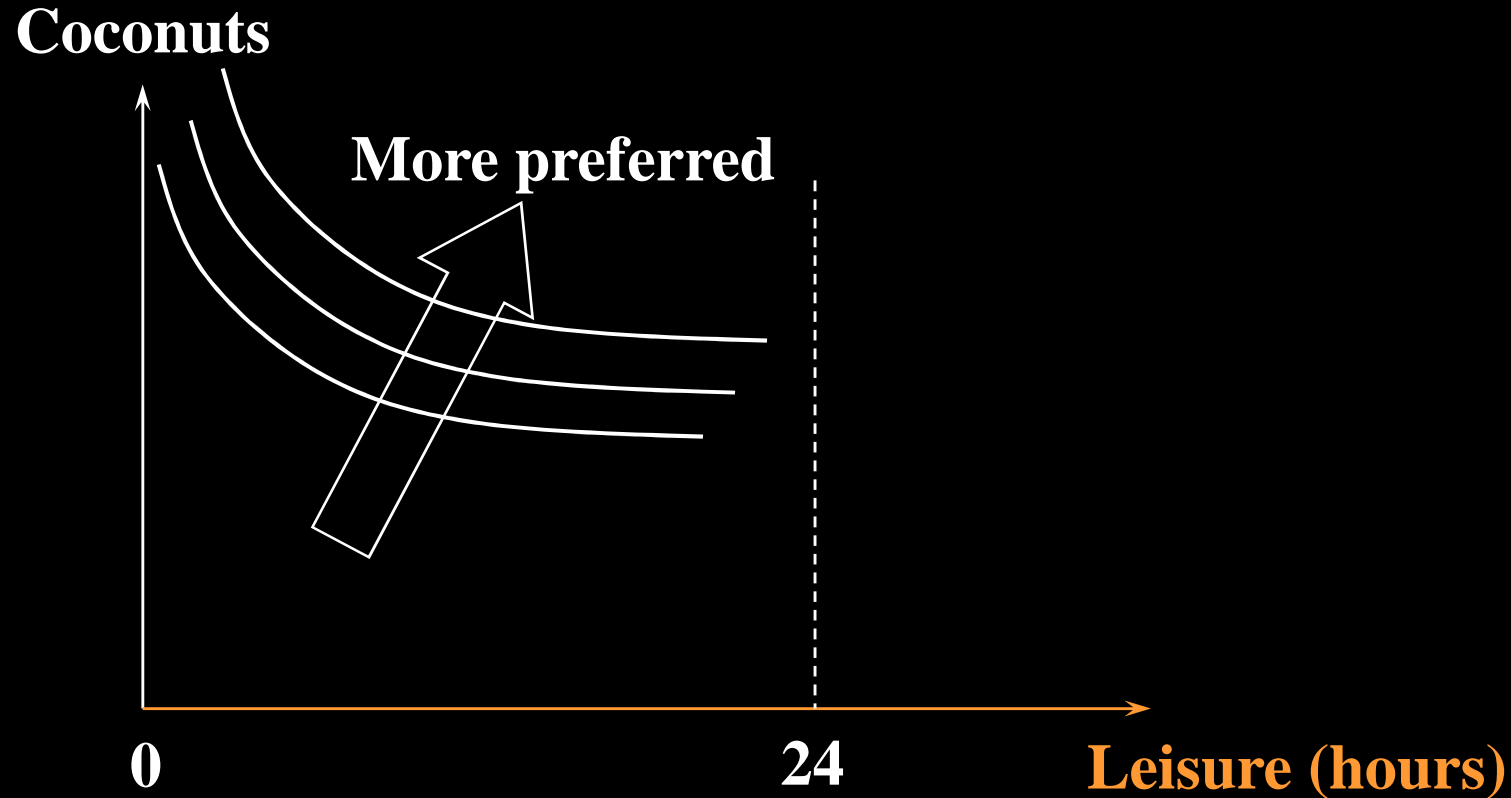
- ◆ One agent, RC.
- ◆ Endowed with a fixed quantity of one resource -- 24 hours.
- ◆ Use time for labor (production) or leisure (consumption).
- ◆ Labor time = L . Leisure time = $24 - L$.
- ◆ What will RC choose?

Robinson Crusoe's Technology



Technology: Labor produces output (coconuts) according to a concave production function.

Robinson Crusoe's Preferences

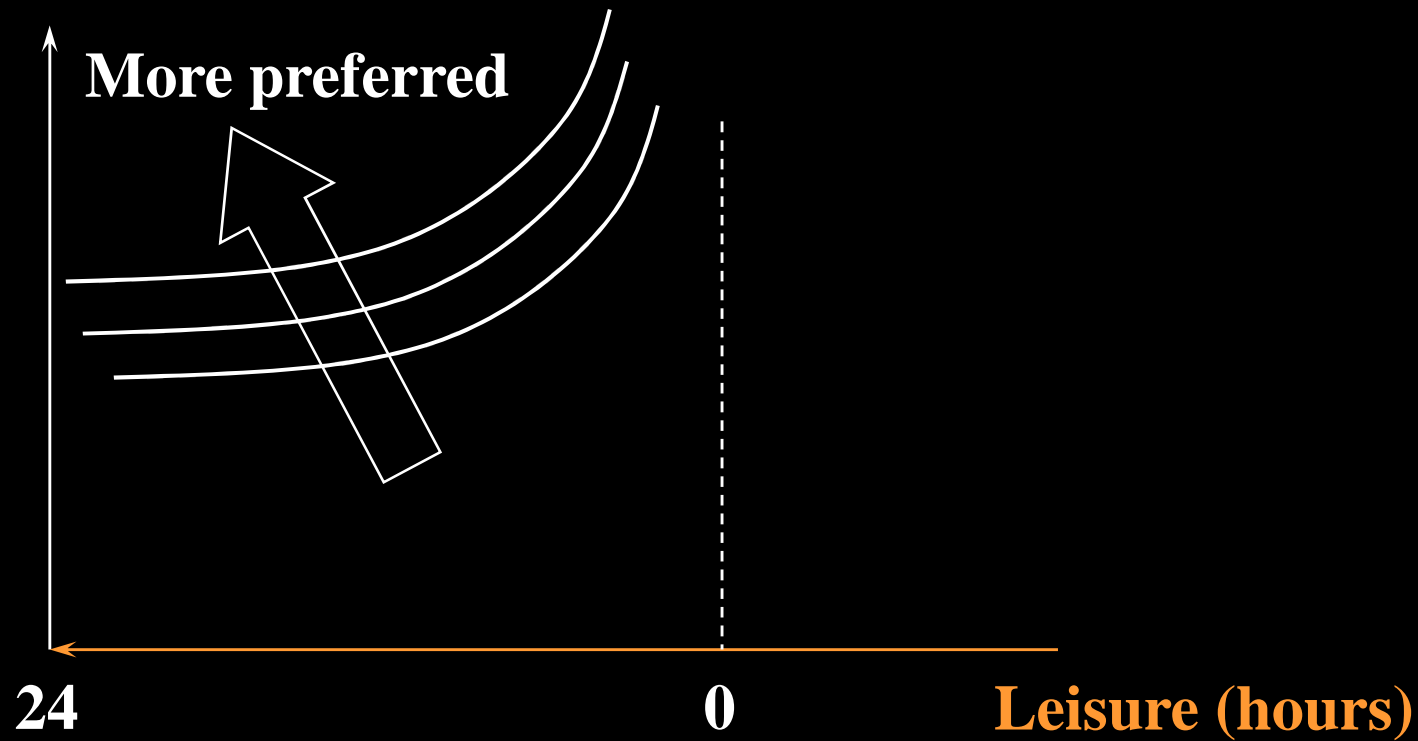


RC's preferences:

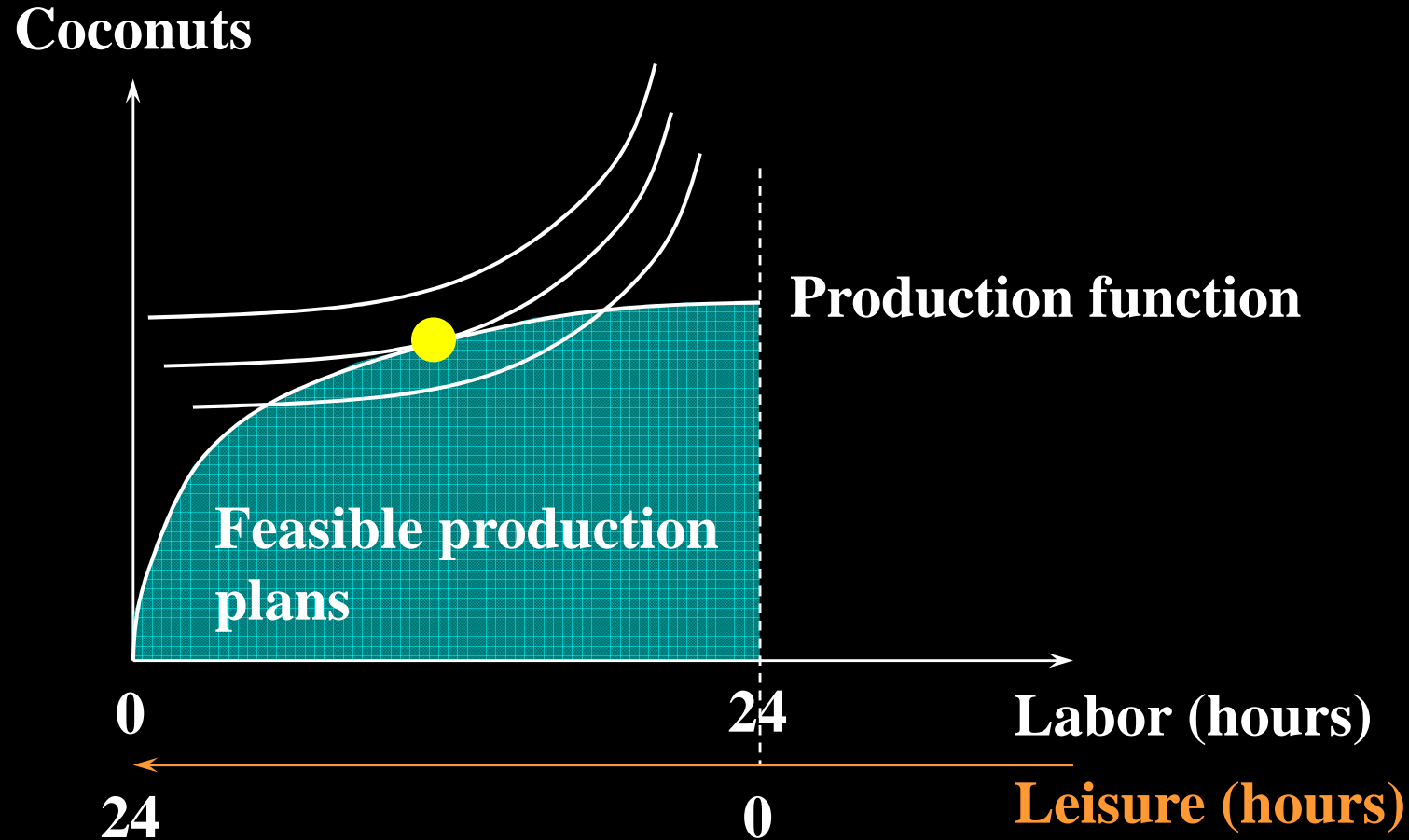
- coconut is a good
- leisure is a good

Robinson Crusoe's Preferences

Coconuts

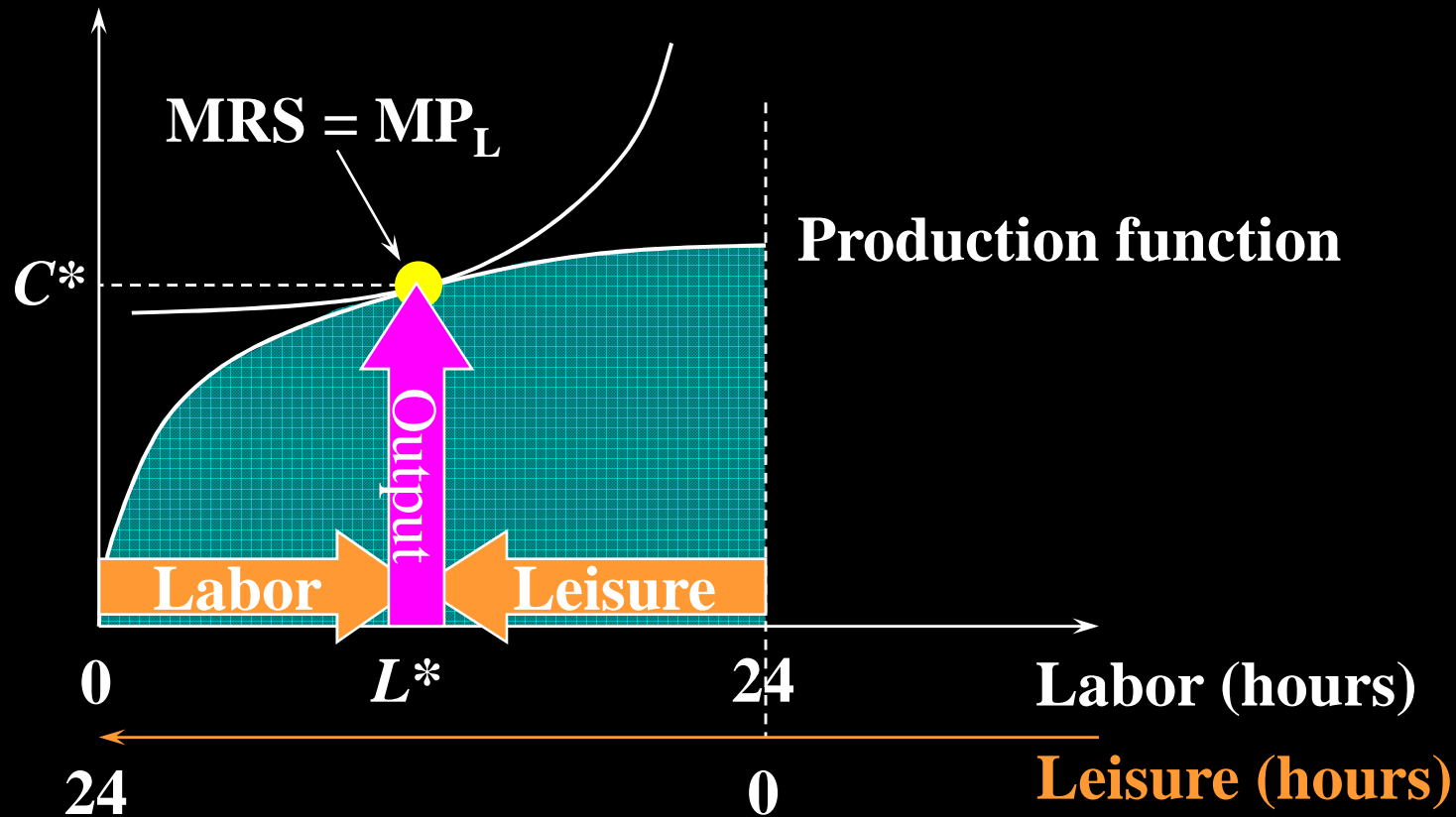


Robinson Crusoe's Choice



Robinson Crusoe's Choice

Coconuts



Robinson Crusoe as a Firm

- ◆ Now suppose RC is both a utility-maximizing consumer and a profit-maximizing firm.
- ◆ Use coconuts as the numeraire good; i.e. price of a coconut = \$1.
- ◆ RC's wage rate is w .
- ◆ Coconut output level is C .

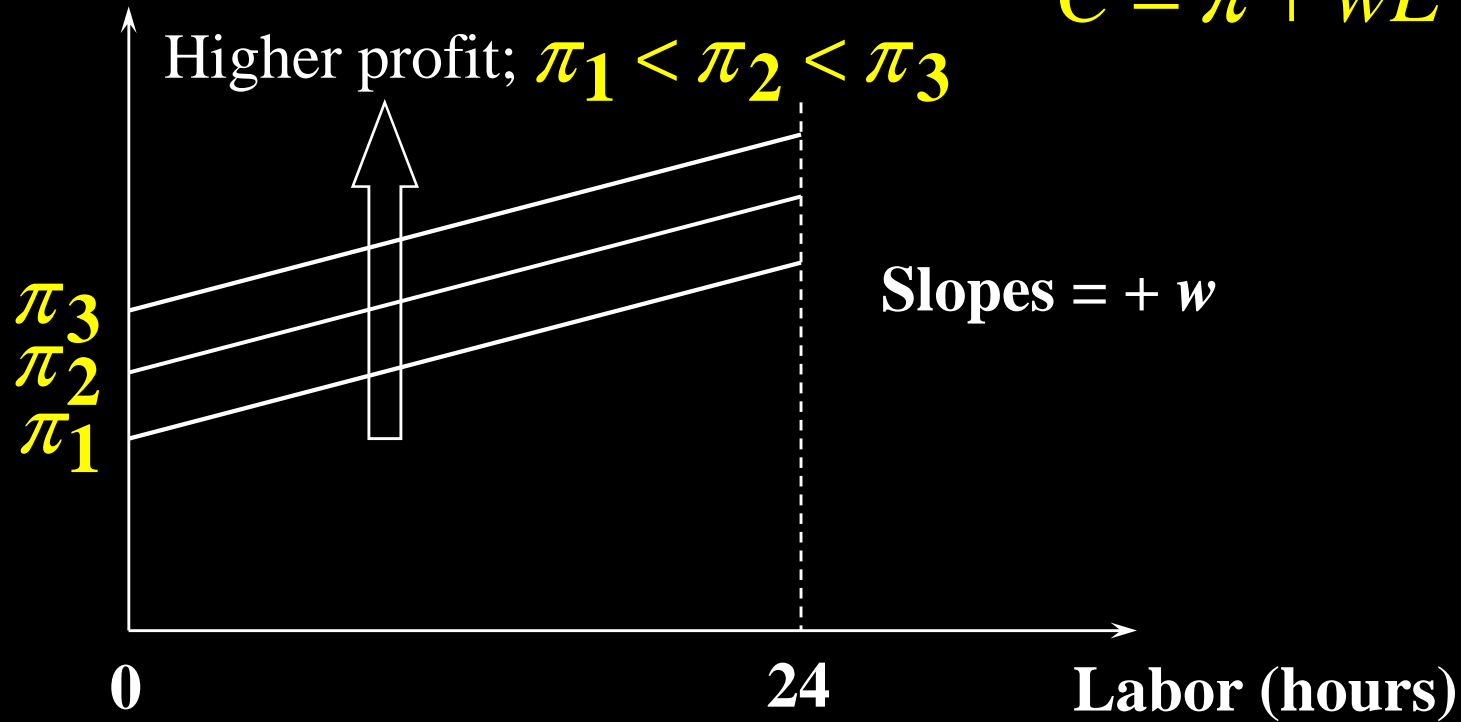
Robinson Crusoe as a Firm

- ◆ RC's firm's profit is $\pi = C - wL$.
- ◆ $\pi = C - wL \Leftrightarrow C = \pi + wL$, the equation of an isoprofit line.
- ◆ Slope = $+ w$.
- ◆ Intercept = π .

Isoprofit Lines

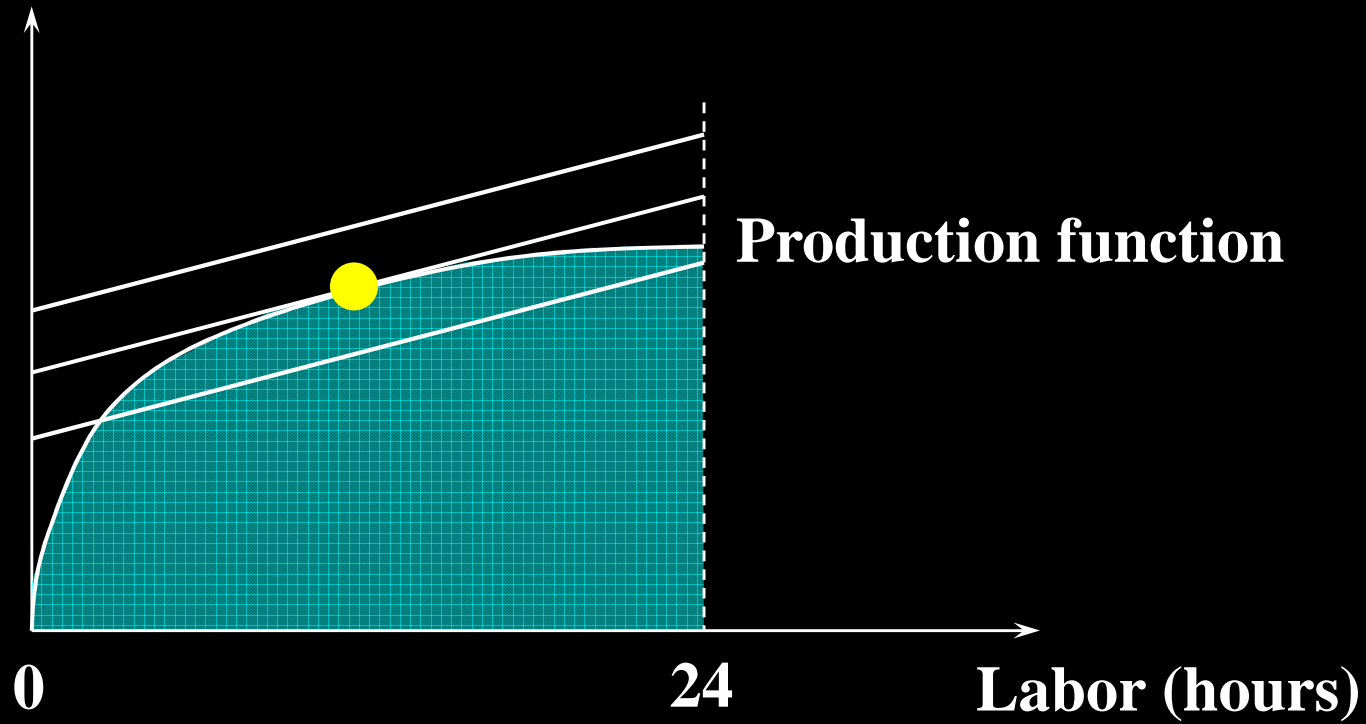
Coconuts

$$C = \pi + wL$$

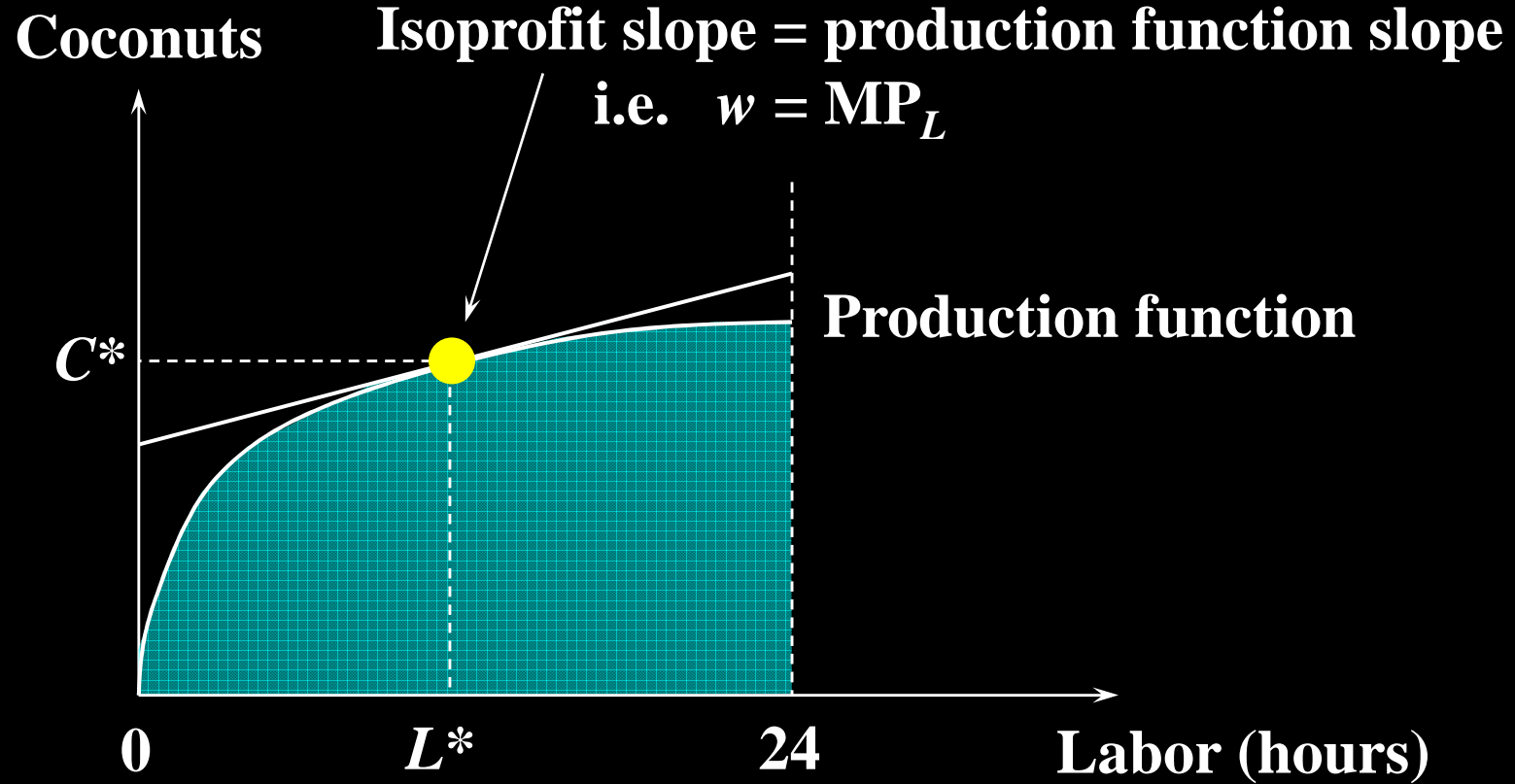


Profit-Maximization

Coconuts



Profit-Maximization

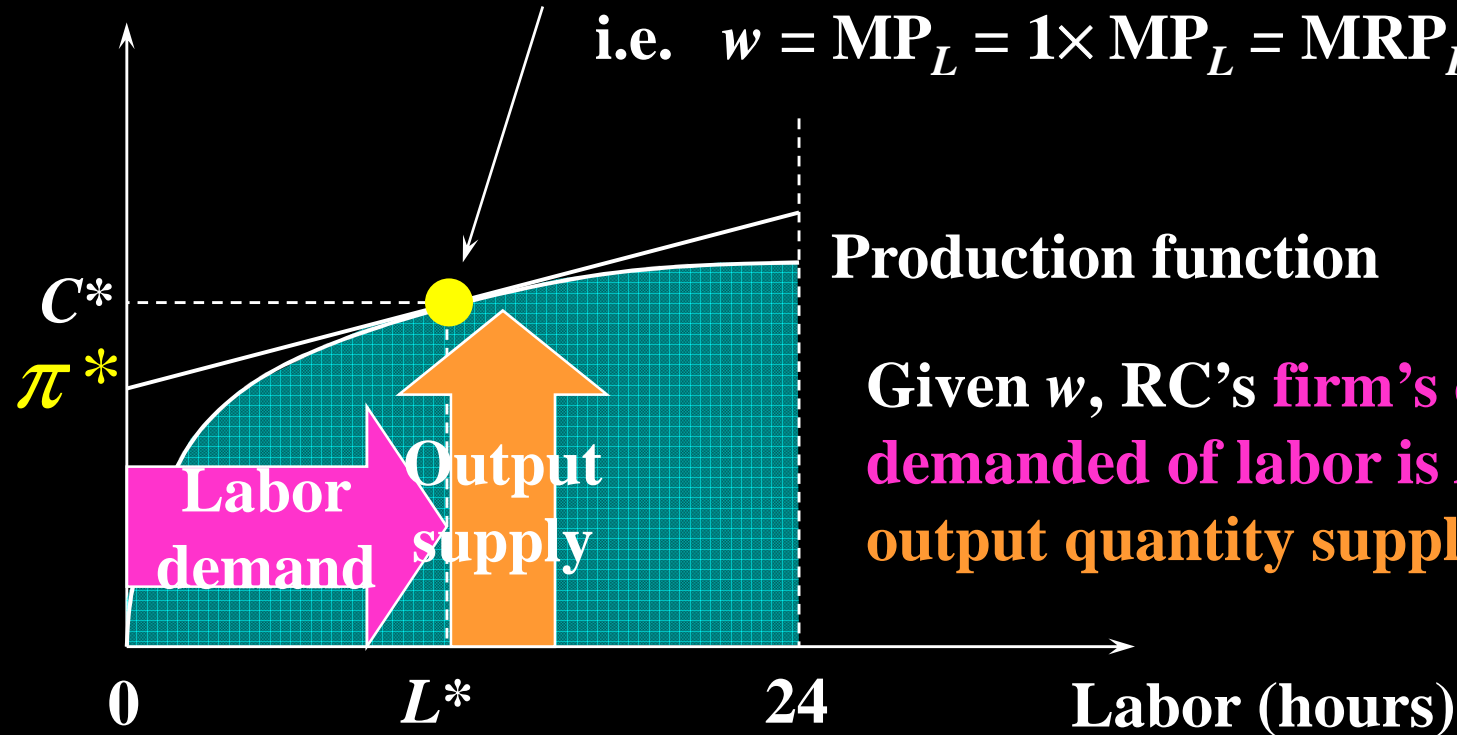


Profit-Maximization

Coconuts

Isoprofit slope = production function slope

i.e. $w = MP_L = 1 \times MP_L = MRP_L$.



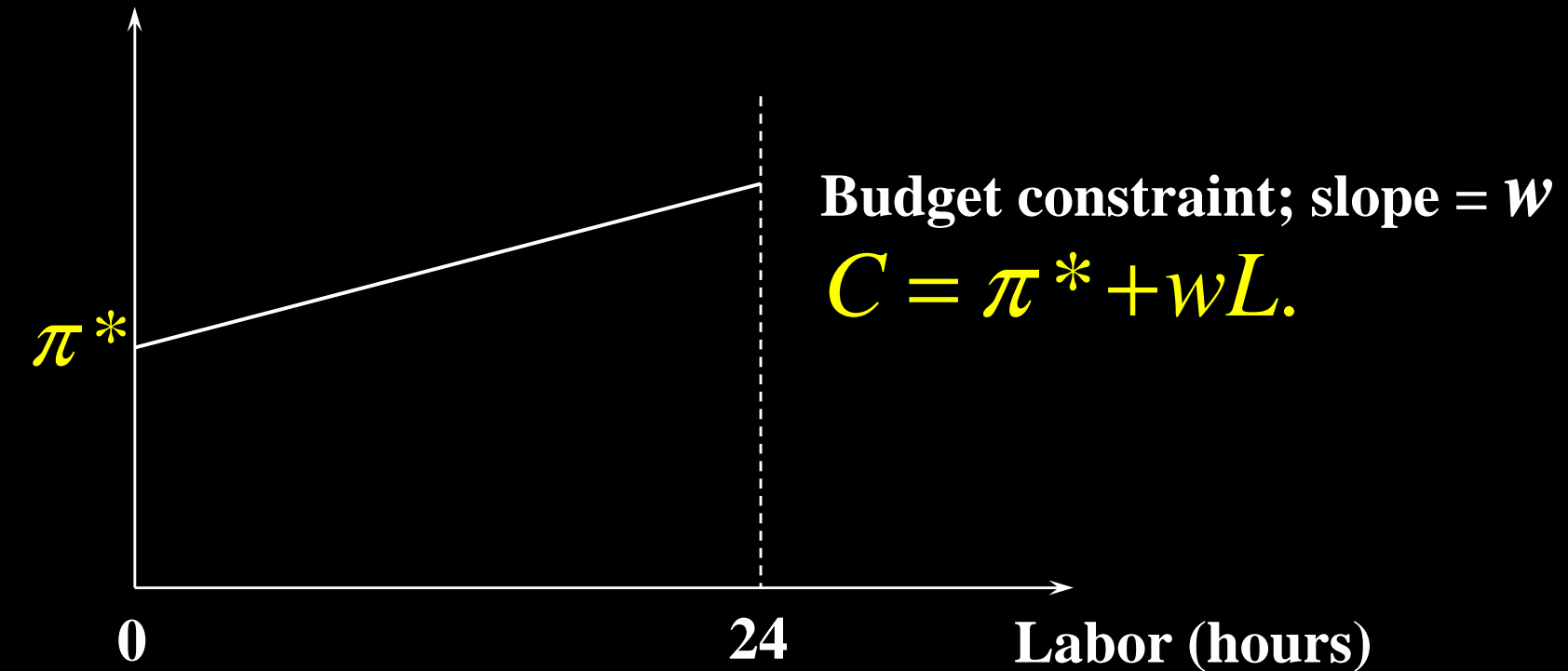
RC gets $\pi^* = C^* - wL^*$

Utility-Maximization

- ◆ Now consider RC as a consumer endowed with π^* who can work for w per hour.
- ◆ What is RC's most preferred consumption bundle?
- ◆ Budget constraint is $C = \pi^* + wL$.

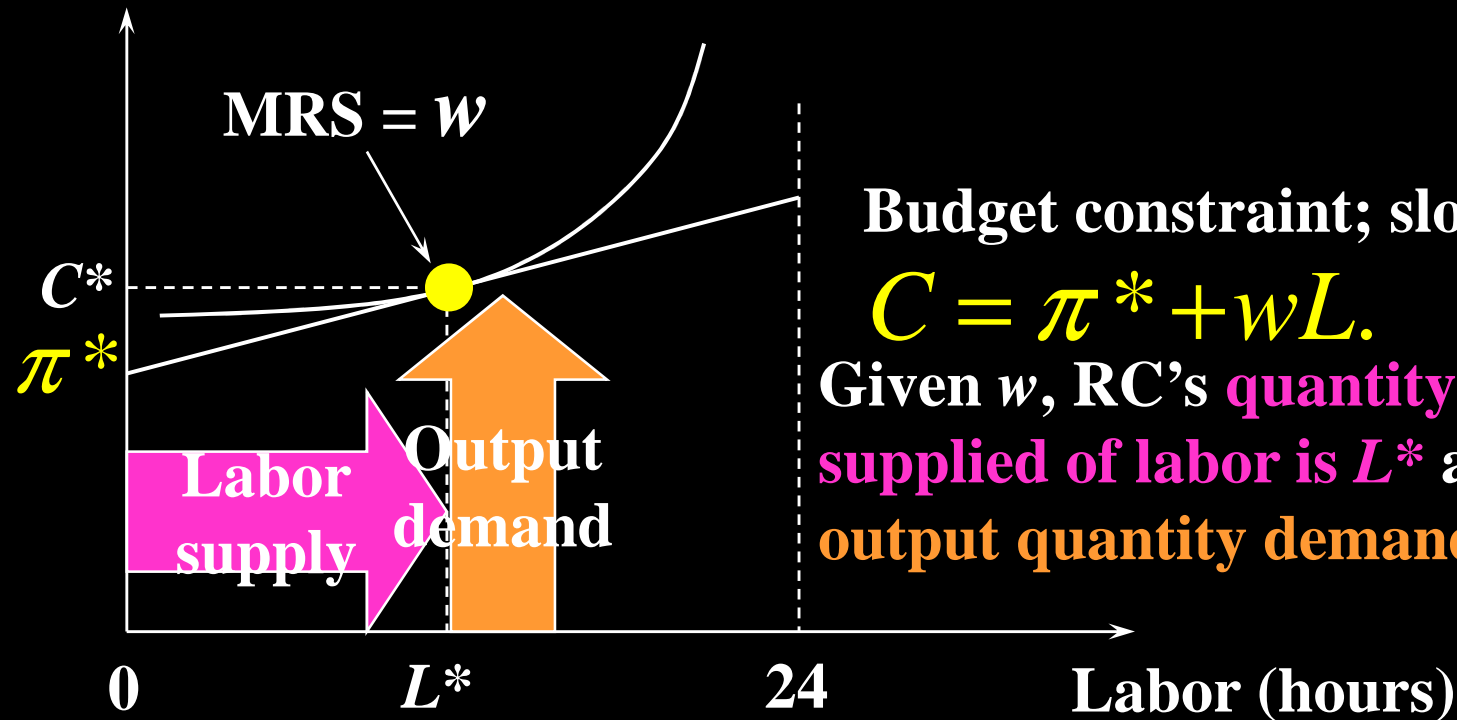
Utility-Maximization

Coconuts



Utility-Maximization

Coconuts



Budget constraint; slope = w

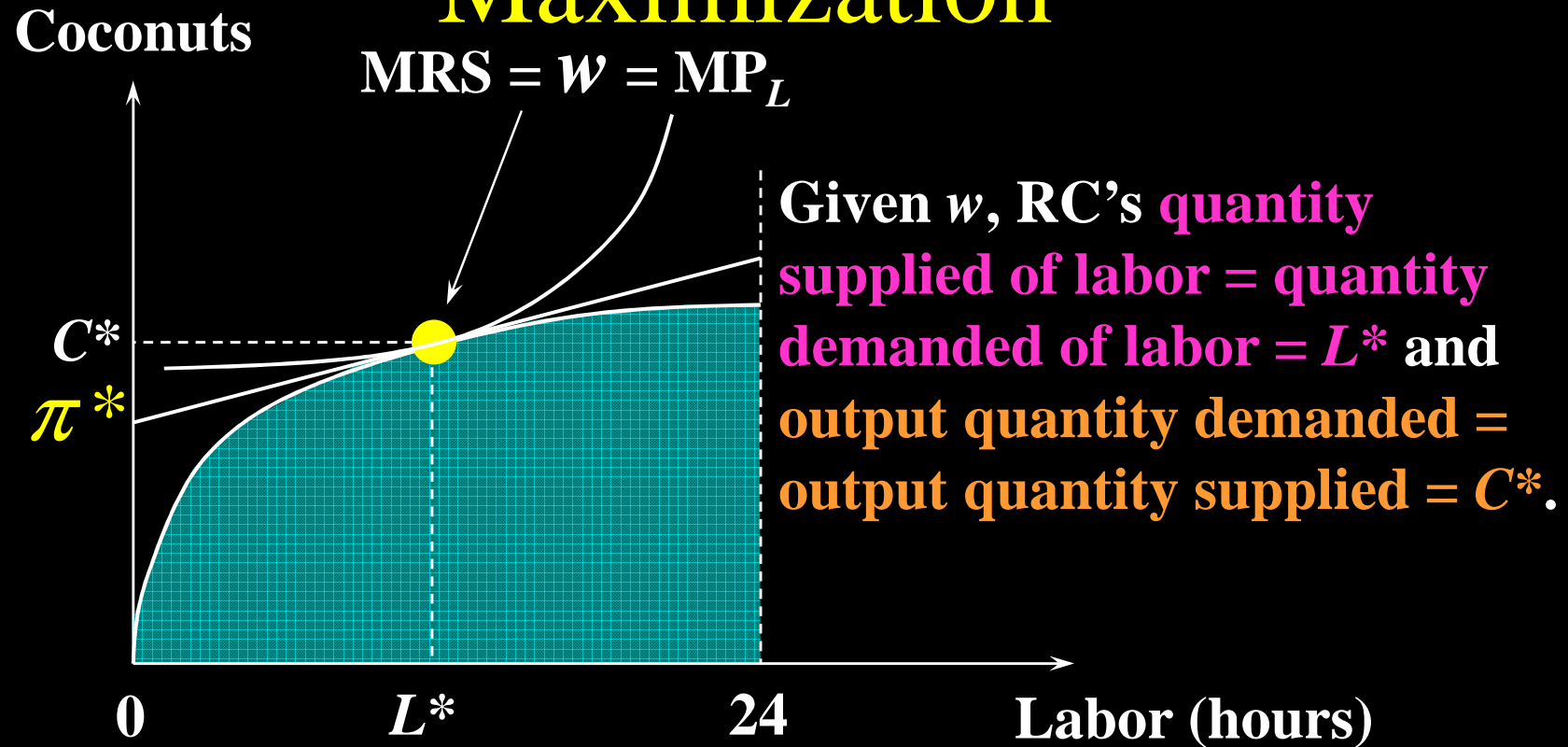
$$C = \pi^* + wL.$$

Given w , RC's **quantity supplied of labor is L^*** and **output quantity demanded is C^*** .

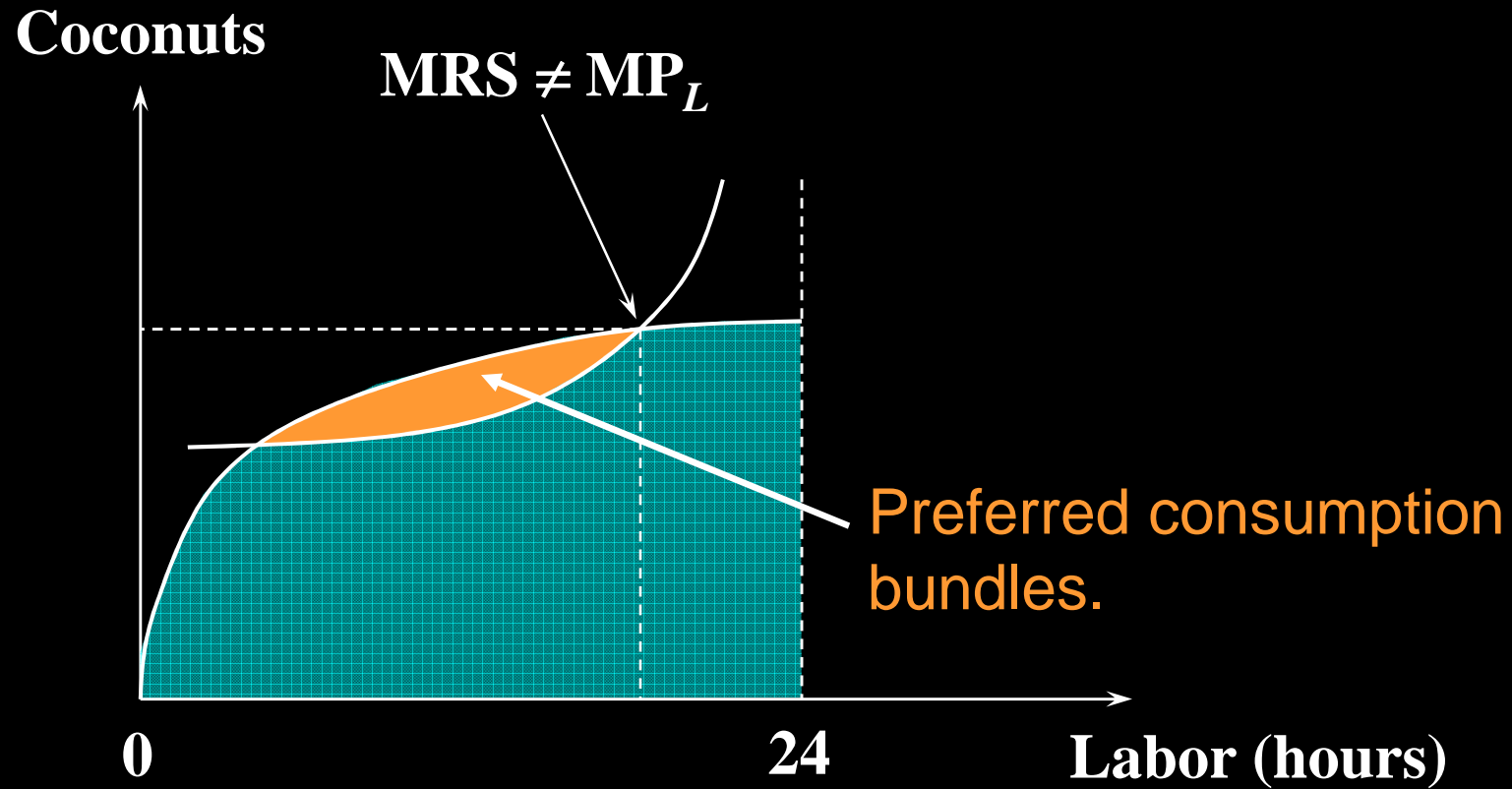
Utility-Maximization & Profit-Maximization

- ◆ Profit-maximization: **Coconut and labor markets both clear.**
 - $w = MP_L$
 - quantity of output supplied = C^*
 - quantity of labor demanded = L^*
- ◆ Utility-maximization:
 - $w = MRS$
 - quantity of output demanded = C^*
 - quantity of labor supplied = L^*

Utility-Maximization & Profit-Maximization



Pareto Efficiency



Production Possibilities

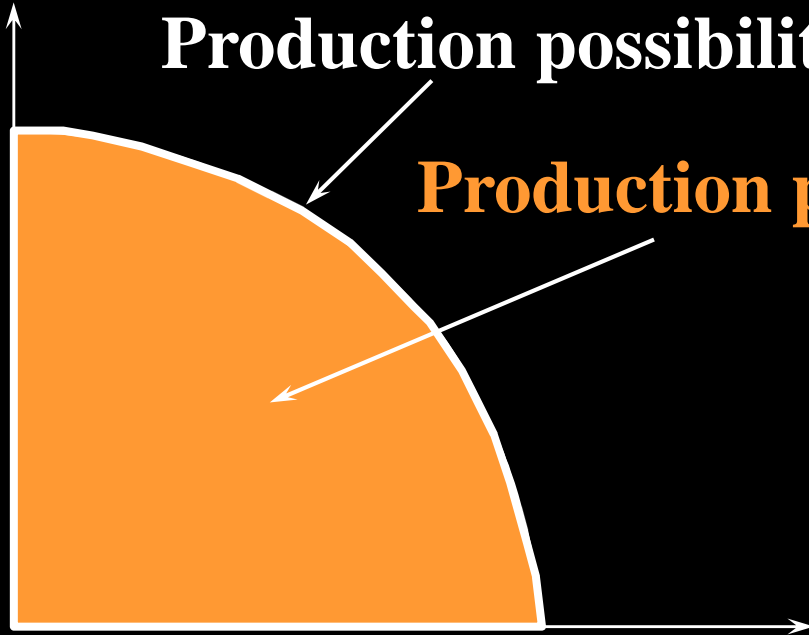
- ◆ Resource and technological limitations restrict what an economy can produce.
- ◆ The set of all feasible output bundles is the economy's **production possibility set**.
- ◆ The set's outer boundary is the **production possibility frontier**.

Production Possibilities

Coconuts

Production possibility frontier (ppf)

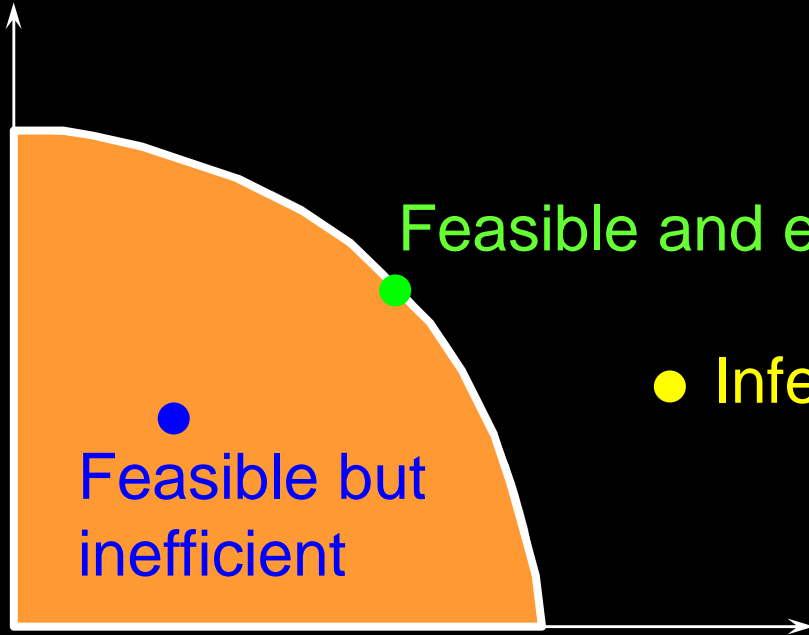
Production possibility set



Fish

Production Possibilities

Coconuts



Feasible and efficient

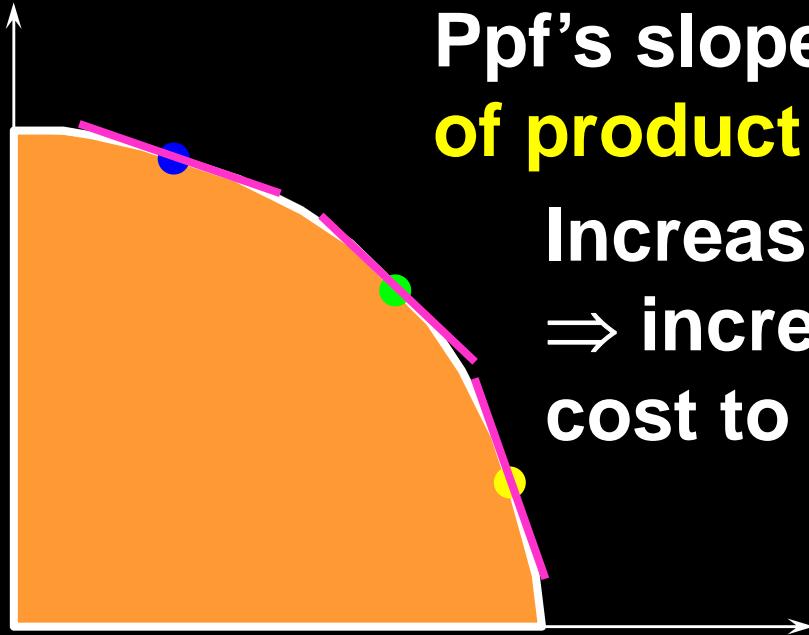
● Infeasible

● Feasible but inefficient

Fish

Production Possibilities

Coconuts



Ppf's slope is the **marginal rate of product transformation**.

Increasingly negative MRPT
⇒ increasing opportunity
cost to specialization.

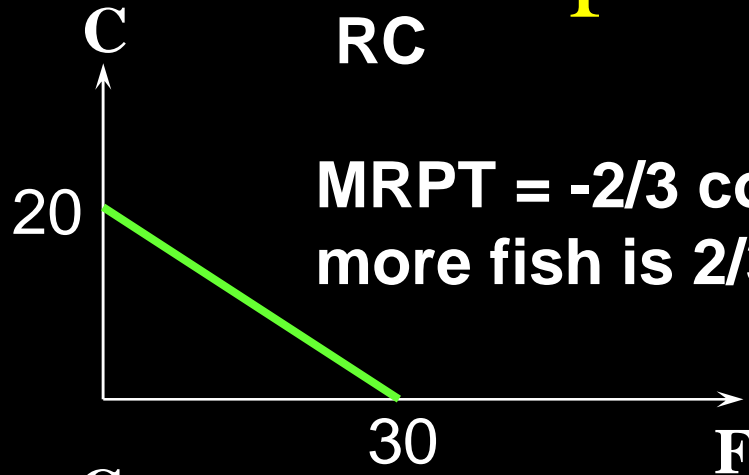
Fish

Comparative Advantage

- ◆ Two agents, RC and Man Friday (MF).
- ◆ RC can produce at most 20 coconuts or 30 fish.
- ◆ MF can produce at most 50 coconuts or 25 fish.

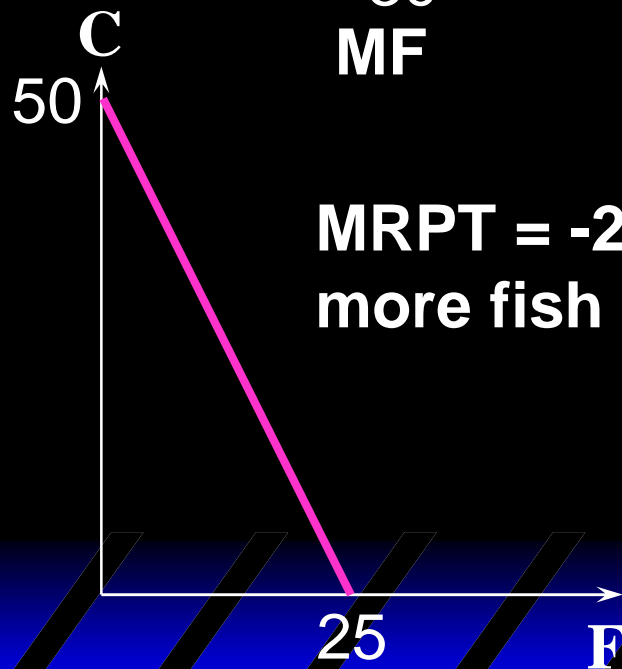
Comparative Advantage

RC



MRPT = $-2/3$ coconuts/fish so opp. cost of one more fish is $2/3$ foregone coconuts.

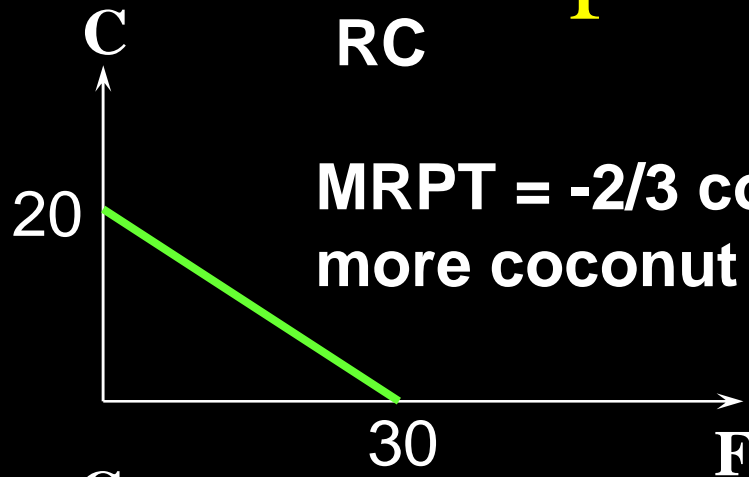
RC has the comparative opp. cost advantage in producing fish.



MRPT = -2 coconuts/fish so opp. cost of one more fish is 2 foregone coconuts.

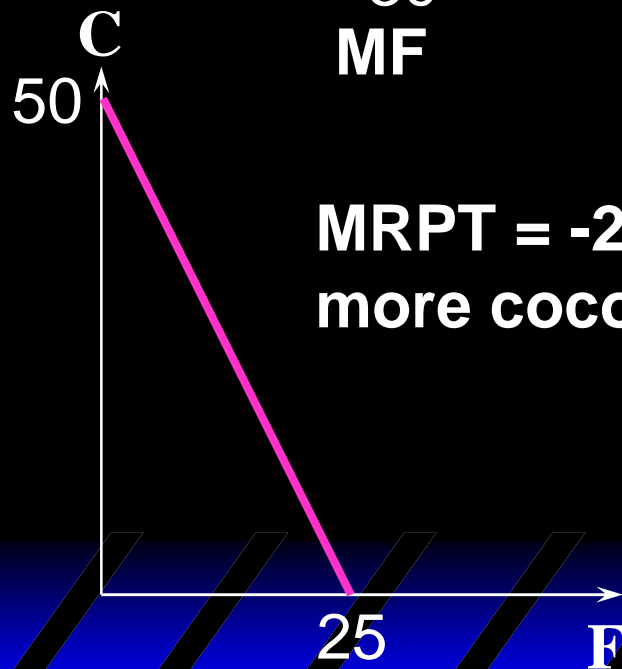
Comparative Advantage

RC



MRPT = $-\frac{2}{3}$ coconuts/fish so opp. cost of one more coconut is $\frac{3}{2}$ foregone fish.

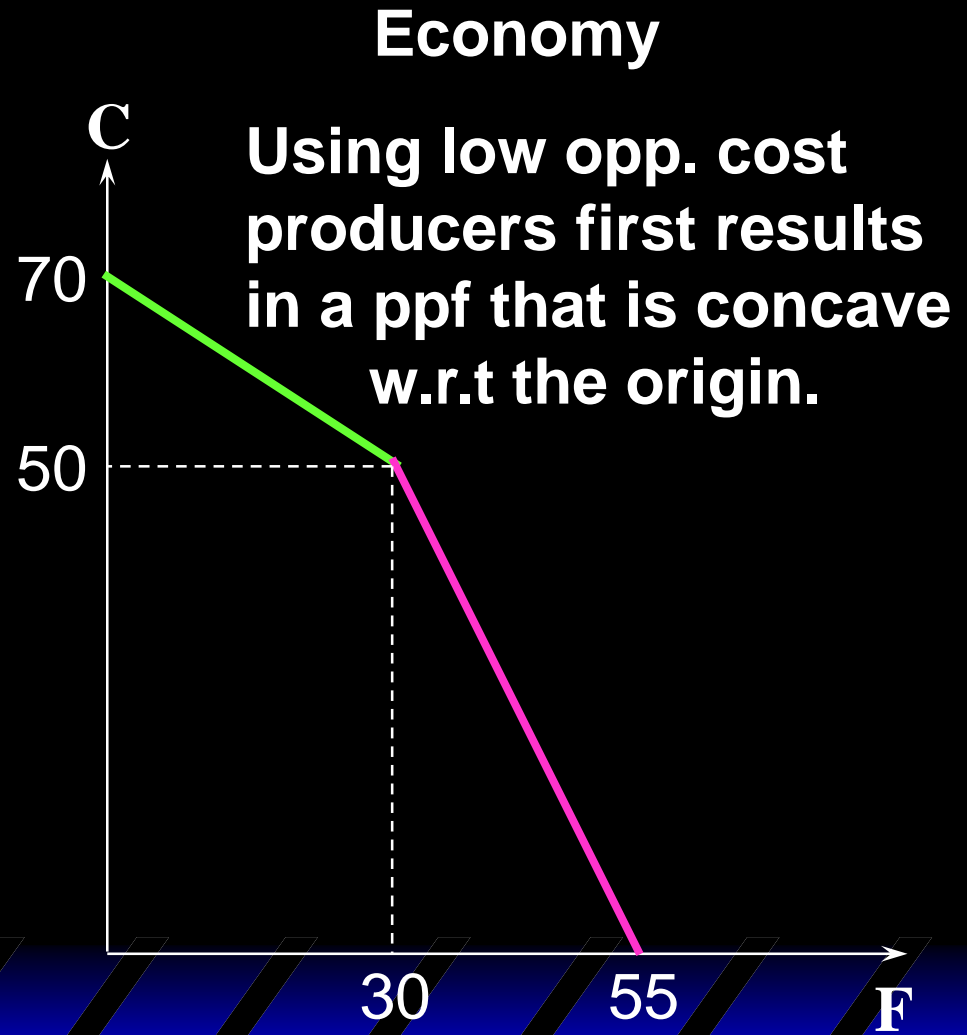
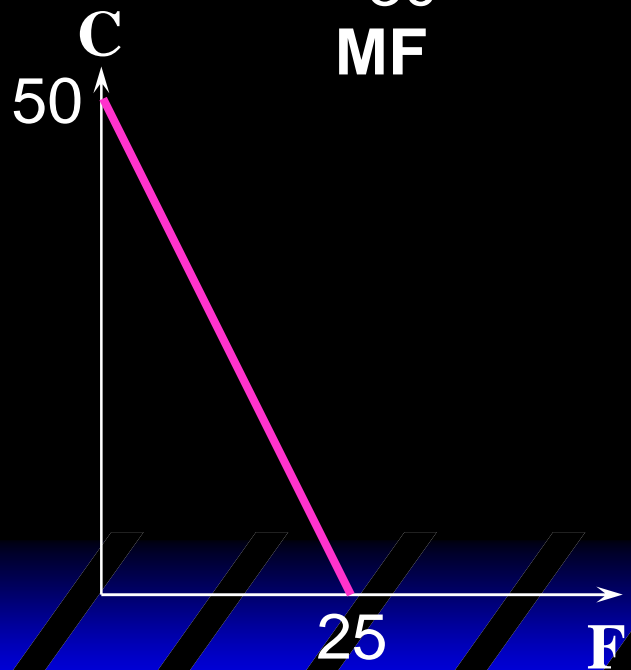
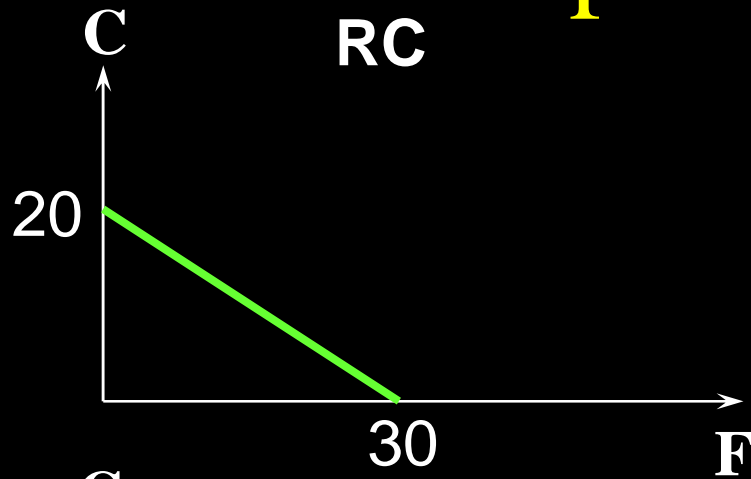
MF



MRPT = -2 coconuts/fish so opp. cost of one more coconut is $\frac{1}{2}$ foregone fish.

MF has the comparative opp. cost advantage in producing coconuts.

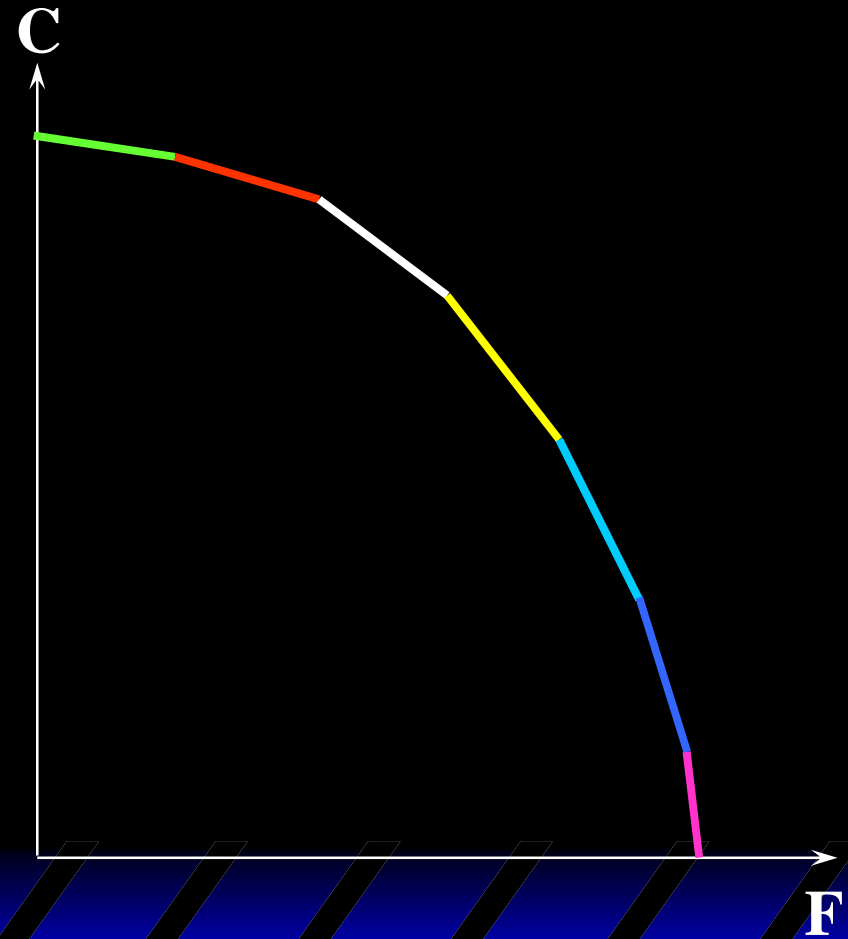
Comparative Advantage



Comparative Advantage

Economy

More producers with
different opp. costs
“smooth out” the ppf.



Coordinating Production & Consumption

- ◆ The ppf contains many technically efficient output bundles.
- ◆ Which are Pareto efficient for consumers?
- ◆ **MRS = MRPT is necessary for a Pareto optimal economic state.**

Decentralized Coordination of Production & Consumption

- ◆ RC and MF jointly run a firm producing coconuts and fish.
- ◆ RC and MF are also consumers who can sell labor.
- ◆ Price of coconut = p_C .
- ◆ Price of fish = p_F .
- ◆ RC's wage rate = w_{RC} .
- ◆ MF's wage rate = w_{MF} .

Decentralized Coordination of Production & Consumption

- ◆ L_{RC} , L_{MF} are amounts of labor purchased from RC and MF.
- ◆ Firm's profit-maximization problem is choose C , F , L_{RC} and L_{MF} to

$$\max \pi = p_C C + p_F F - w_{RC} L_{RC} - w_{MF} L_{MF}.$$

Decentralized Coordination of Production & Consumption

$$\max \pi = p_C C + p_F F - w_{RC} L_{RC} - w_{MF} L_{MF} \cdot$$

Isoprofit line equation is

$$\text{constant } \pi = p_C C + p_F F - w_{RC} L_{RC} - w_{MF} L_{MF}$$

which rearranges to

$$C = \underbrace{\frac{\pi + w_{RC} L_{RC} + w_{MF} L_{MF}}{p_C}}_{\text{intercept}} - \underbrace{\frac{p_F}{p_C}}_{\text{slope}} F$$

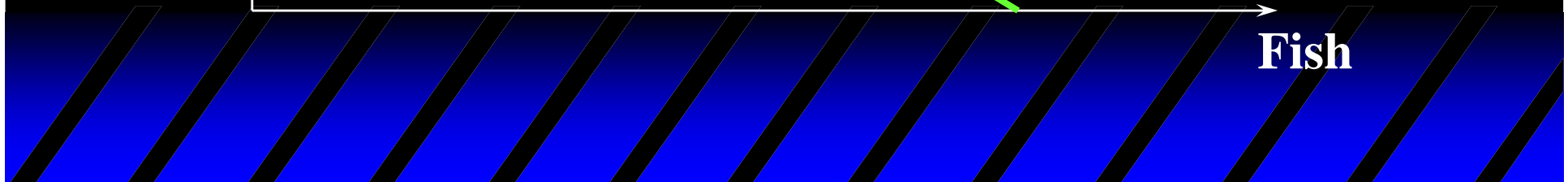
Decentralized Coordination of Production & Consumption

Coconuts

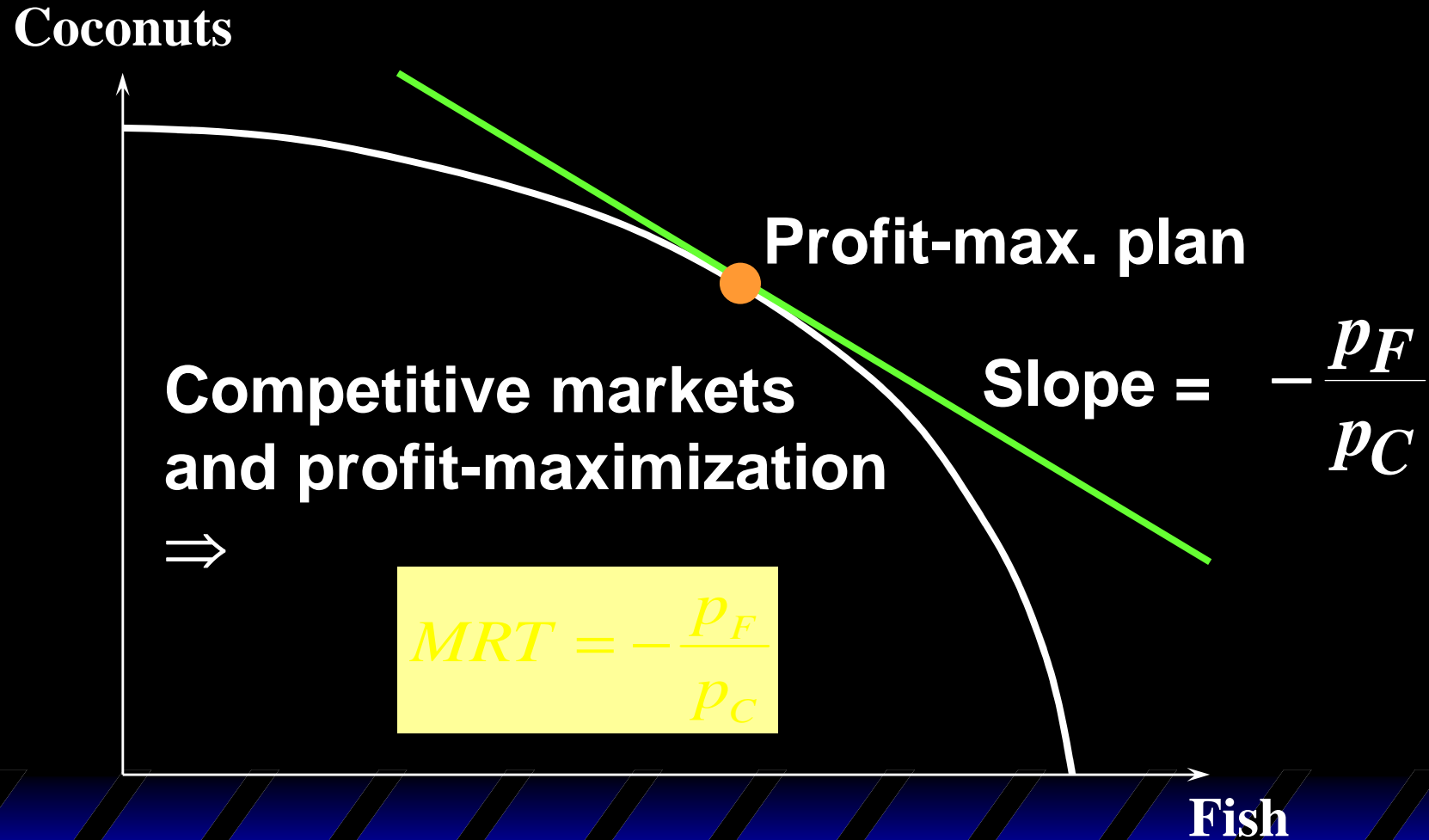
Higher profit

$$\text{Slopes} = -\frac{p_F}{p_C}$$

Fish



Decentralized Coordination of Production & Consumption



Decentralized Coordination of Production & Consumption

- ◆ So competitive markets, profit-maximization, and utility maximization all together cause

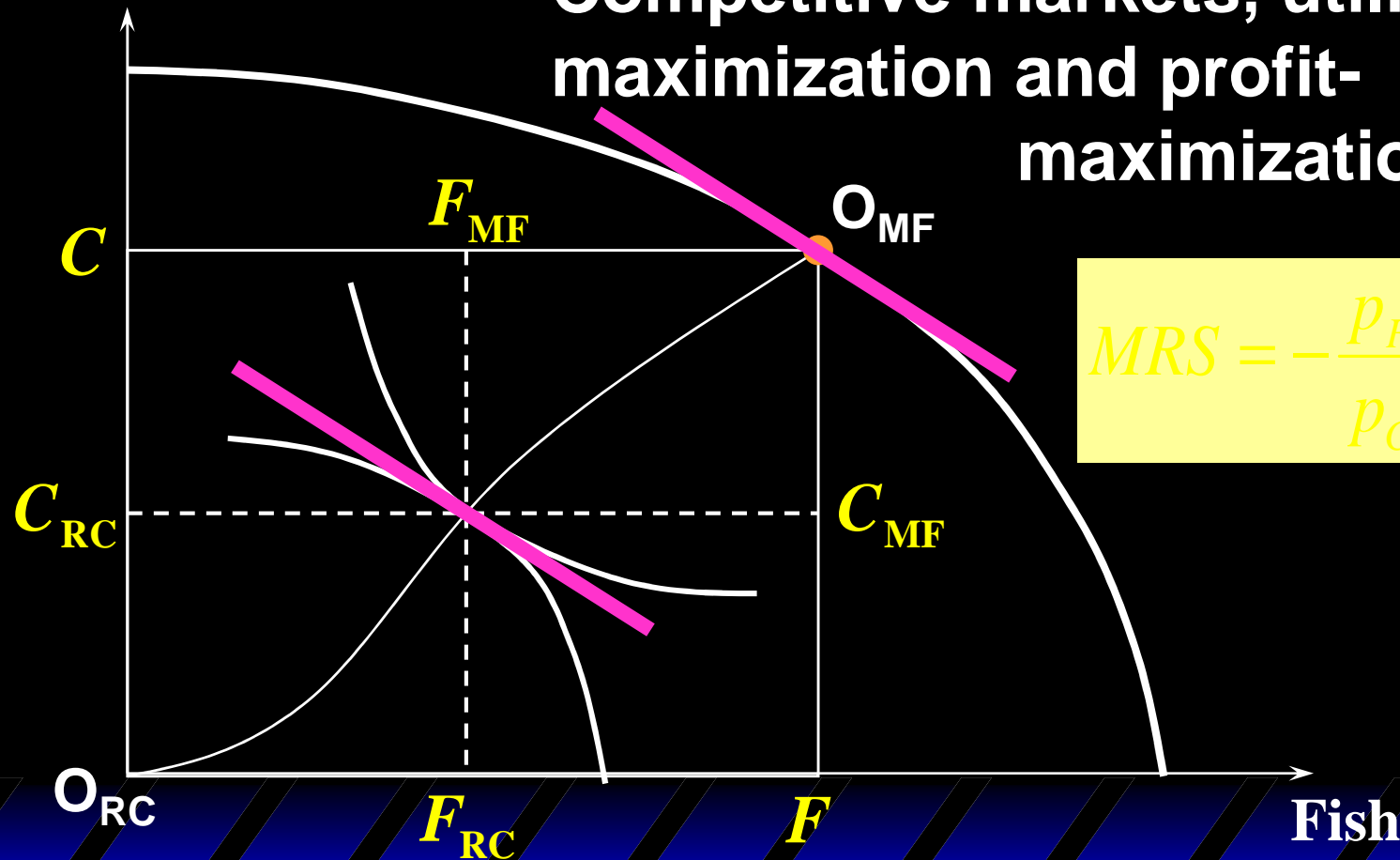
$$MRT = -\frac{P_F}{P_C} = MRS$$

the condition necessary for a Pareto optimal economic state.

Decentralized Coordination of Production & Consumption

Coconuts

Competitive markets, utility-maximization and profit-maximization \Rightarrow



$$MRS = -\frac{P_F}{P_C} = MRT$$